

# The Muon $g-2$ Experiment at Fermilab

Kevin Lynch

*For the Muon  $g-2$  Collaboration*

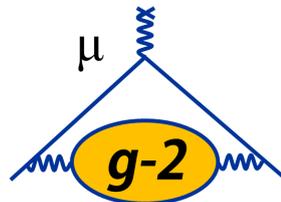
NuFact 2015

Centro Brasileiro de Pesquisas

Físicas

Rio de Janeiro, Brazil

August 10-15, 2015



# Muon g-2 holds a prominent place in the near term US HEP program

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## Building for Discovery

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Strategic Plan for U.S. Particle Physics in the Global Context

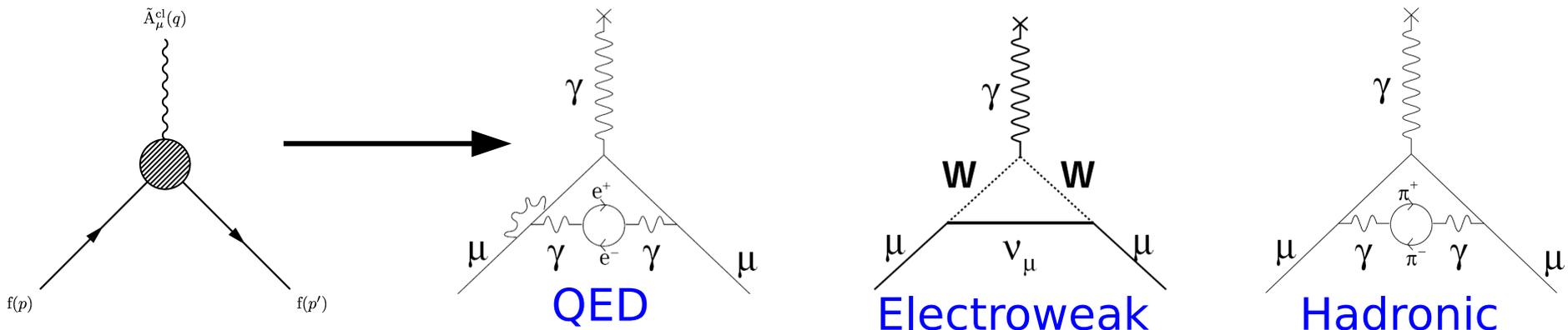
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P5 Report  
Recommendation 22:  
Complete the Mu2e and  
Muon g-2 projects.

Why this emphasis  
on muon physics?

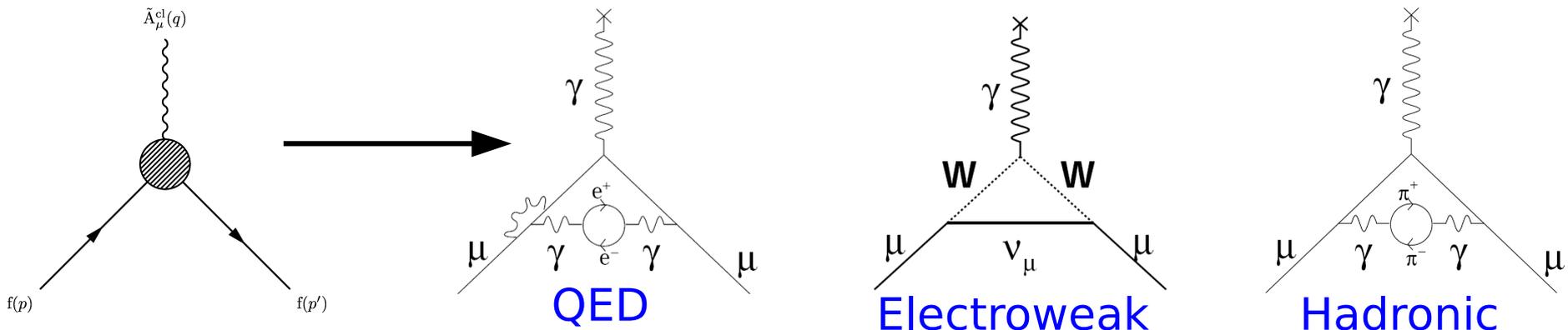
# Muon g-2 is interesting precisely because theorists can calculate it!



$$a_{\mu}^{SM} = a_{\mu}^{QED} + a_{\mu}^{EW} + a_{\mu}^{HLBL} + a_{\mu}^{HVP} + a_{\mu}^{HOHVP} + a_{\mu}^{NP}$$

	VALUE ( $\times 10^{-11}$ ) UNITS
QED ( $\gamma + \ell$ )	$116\,584\,718.853 \pm 0.022 \pm 0.029_{\alpha}$
HVP(lo)*	$6\,923 \pm 42$
HVP(ho)**	$-98.4 \pm 0.7$
H-LBL†	$105 \pm 26$
EW	$153.6 \pm 1.0$
<b>Total SM</b>	$116\,591\,802 \pm 42_{H-LO} \pm 26_{H-HO} \pm 2_{other} (\pm 49_{tot})$

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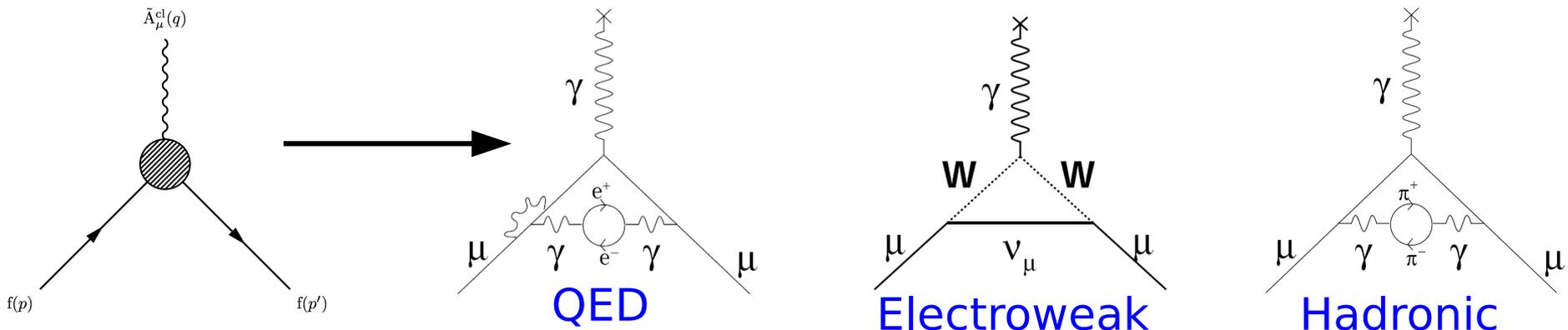


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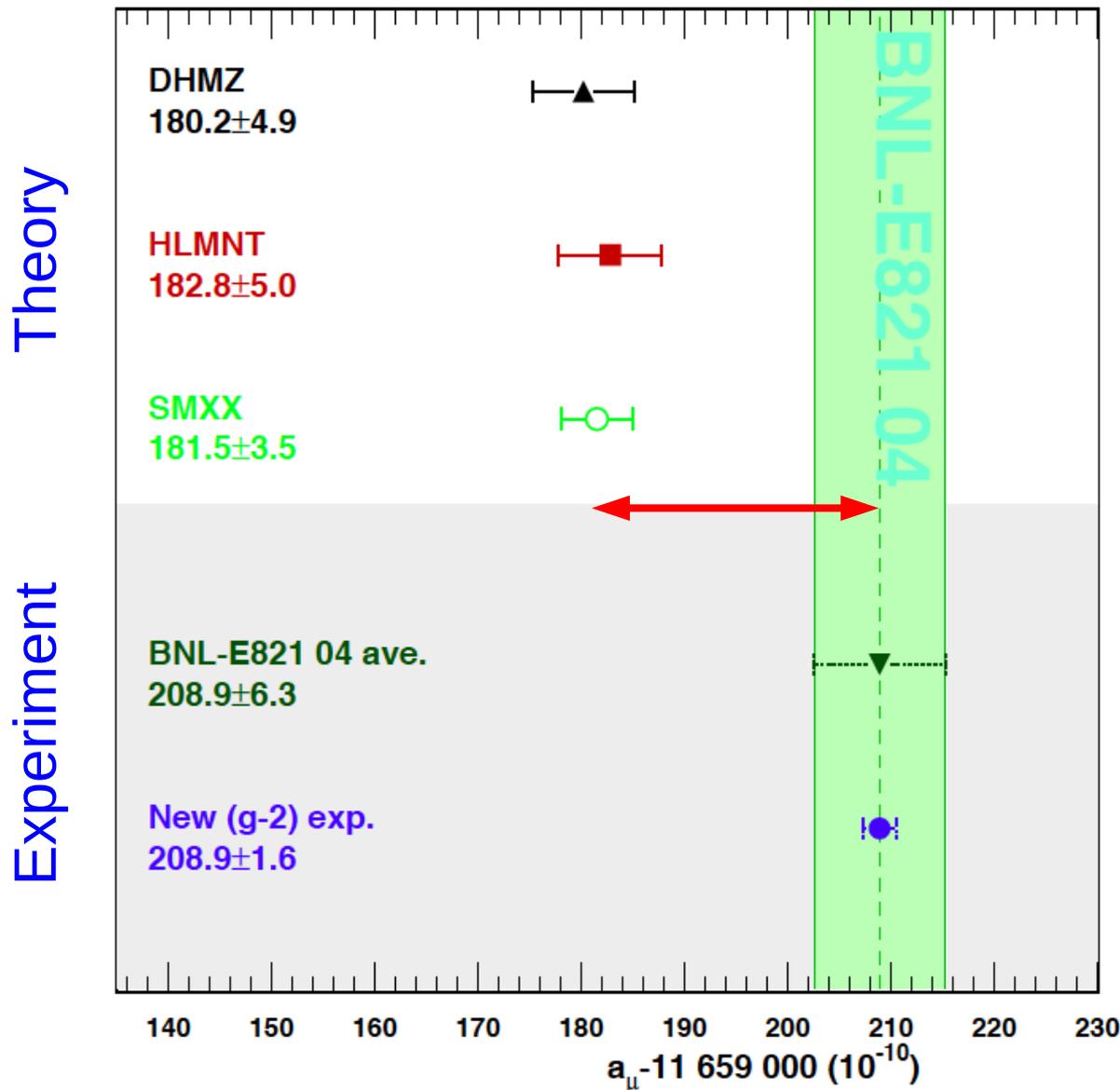
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QED dominates the value

But hadrons dominate the uncertainty

# Muon $g-2$ can both be calculated and measured to fabulously high precision



These error bars are all smaller than 1ppm

The theory/experiment discrepancy currently sits at  $3.6\sigma$

# We achieve this experimental precision because we measure frequencies

If we put a point charged fermion into motion in a plane transverse to a pure magnetic dipole field, both the momentum and the spin precess

Momentum precession – cyclotron motion:

$$\frac{d\vec{p}}{dt} = e\vec{v} \times \vec{B} \longrightarrow \omega_C = \frac{eB}{\gamma mc}$$

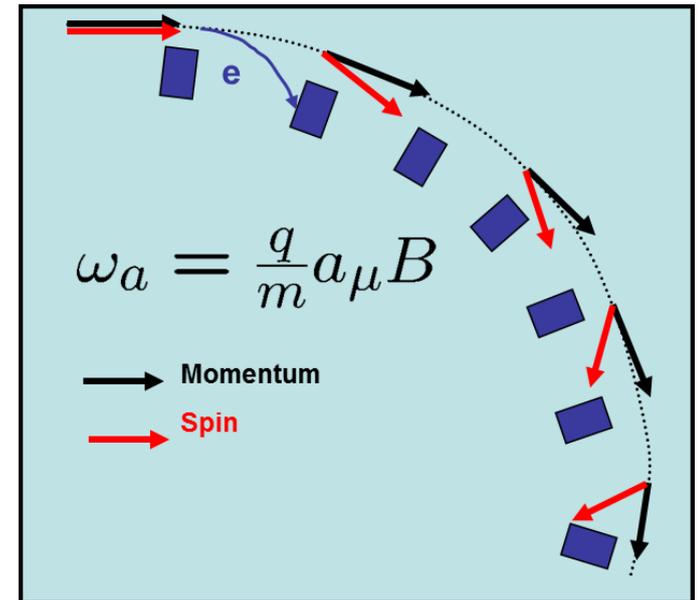
Spin precession – Larmor plus Thomas motion:

$$\frac{d\vec{s}}{dt} = \vec{\mu} \times \vec{B} \longrightarrow \omega_s = \frac{geB}{2mc} + (1 - \gamma) \frac{eB}{\gamma mc}$$

# We achieve this experimental precision because we measure frequencies

The difference between these two comes from an *anomalous magnetic moment* not predicted by pure Dirac theory

$$\omega_a = \omega_C - \omega_s = \left( \frac{g - 2}{2} \right) \frac{eB}{mc} = a_\mu \frac{eB}{mc}$$



If we're a little more careful and include other moments and fields, the frequency to be measured becomes more complicated

$$\vec{\omega}_a = \frac{e}{mc} \left( a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} - a_\mu \frac{\gamma}{\gamma + 1} (\vec{\beta} \cdot \vec{B}) \vec{\beta} \right)$$

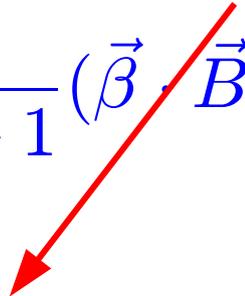
We can address these additional terms  
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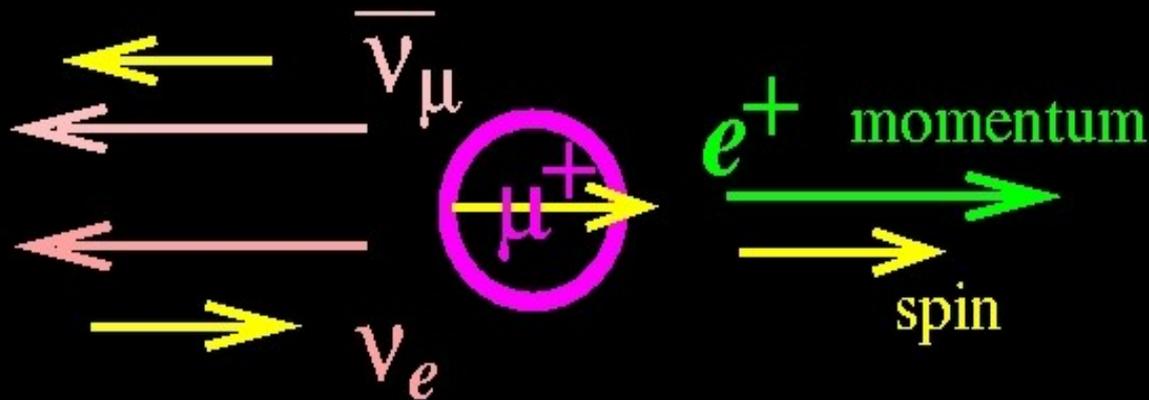
There are, of course, small corrections that must be applied for deviations from these ideals, but they are small, well understood, and well controlled.

# Muon decays are self-analyzing for the spin orientation

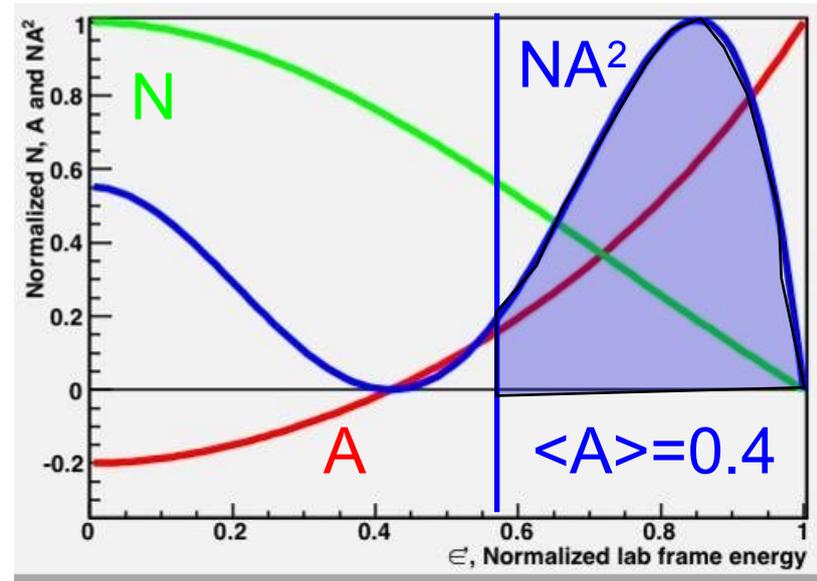
The same chirality violating SM weak physics that produces polarized muon beams in pion decay imprints the muon spin on the electron momentum

$$\frac{d^2\Gamma_{\mu}^{\pm}}{dyd\Omega} = n(y) (1 \mp a(y)\cos\theta)$$

## The Muon Rest Frame



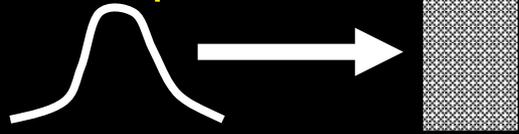
Highest energy  $e^+$  are along muon spin  
The positron carries the muon spin



# Experimental Technique

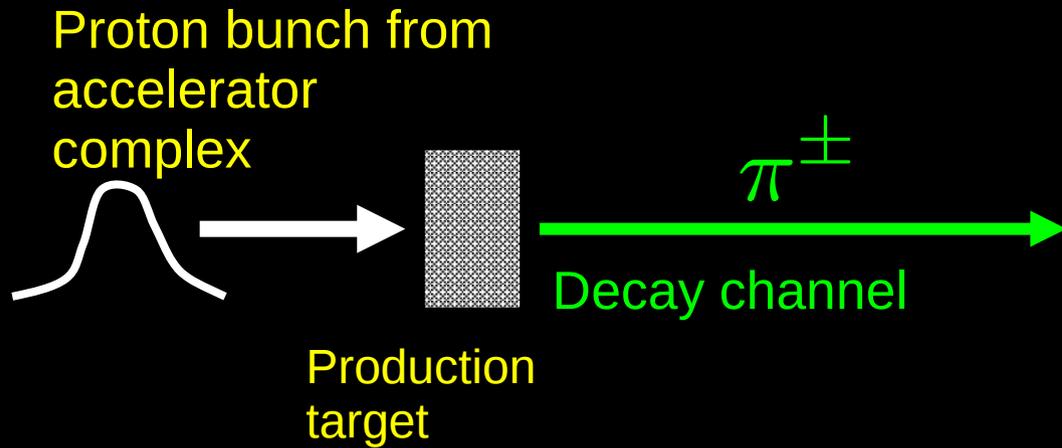
# Experimental Technique

Proton bunch from  
accelerator  
complex

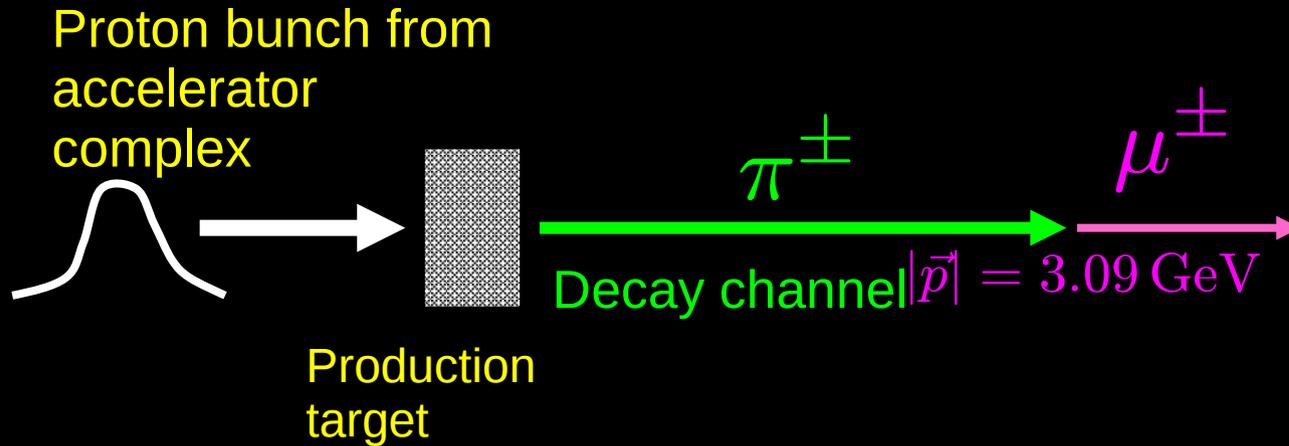


Production  
target

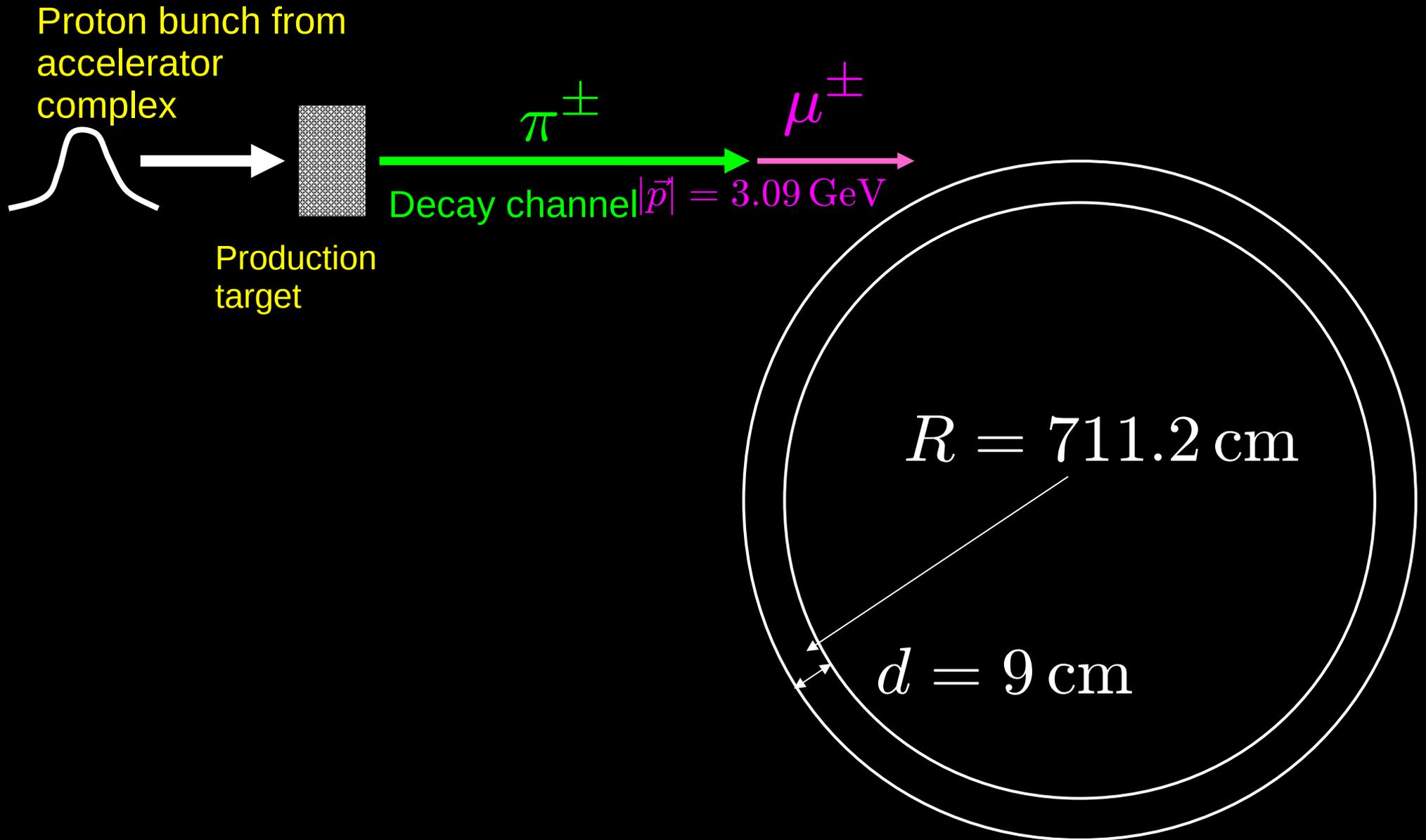
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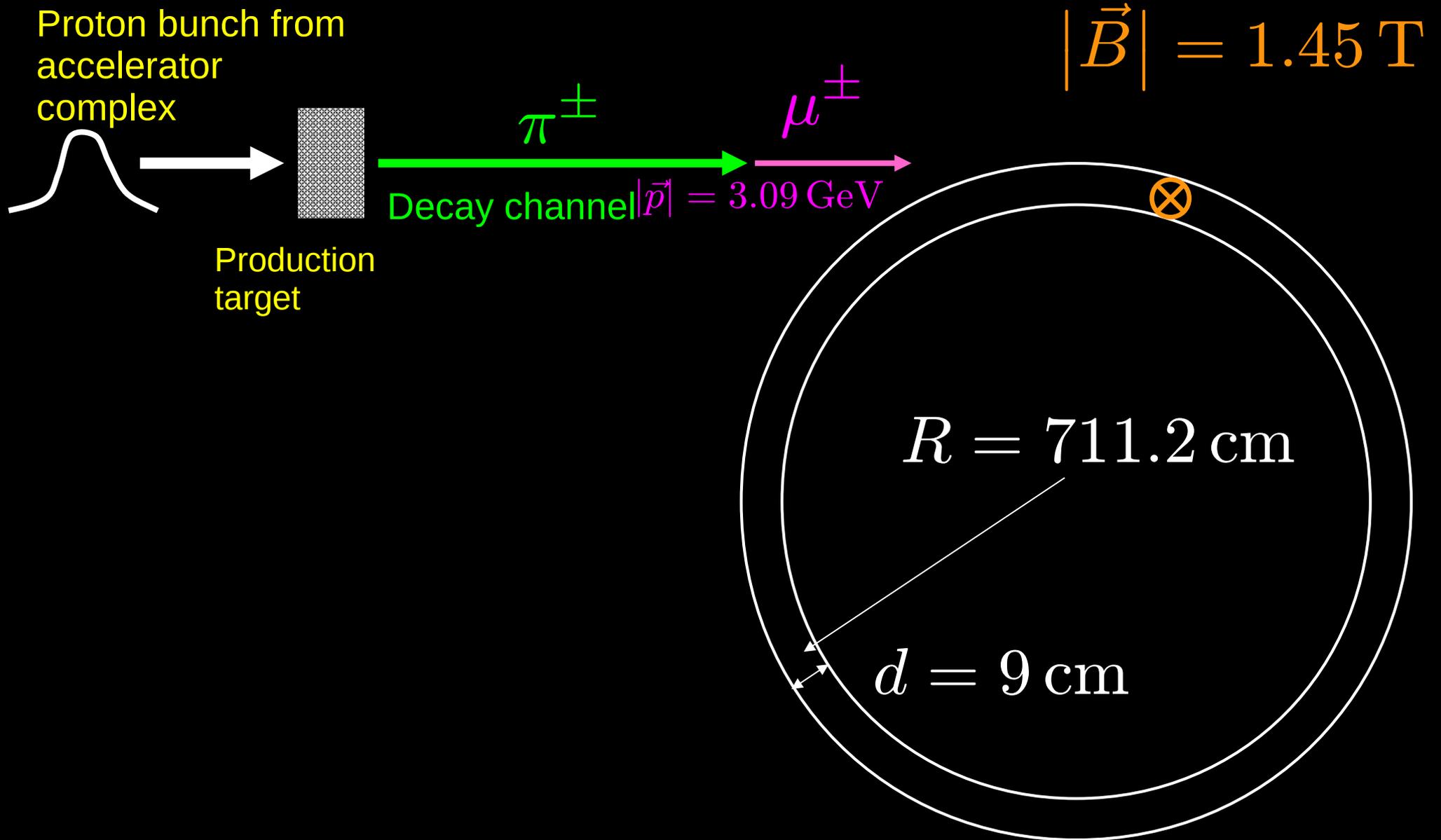
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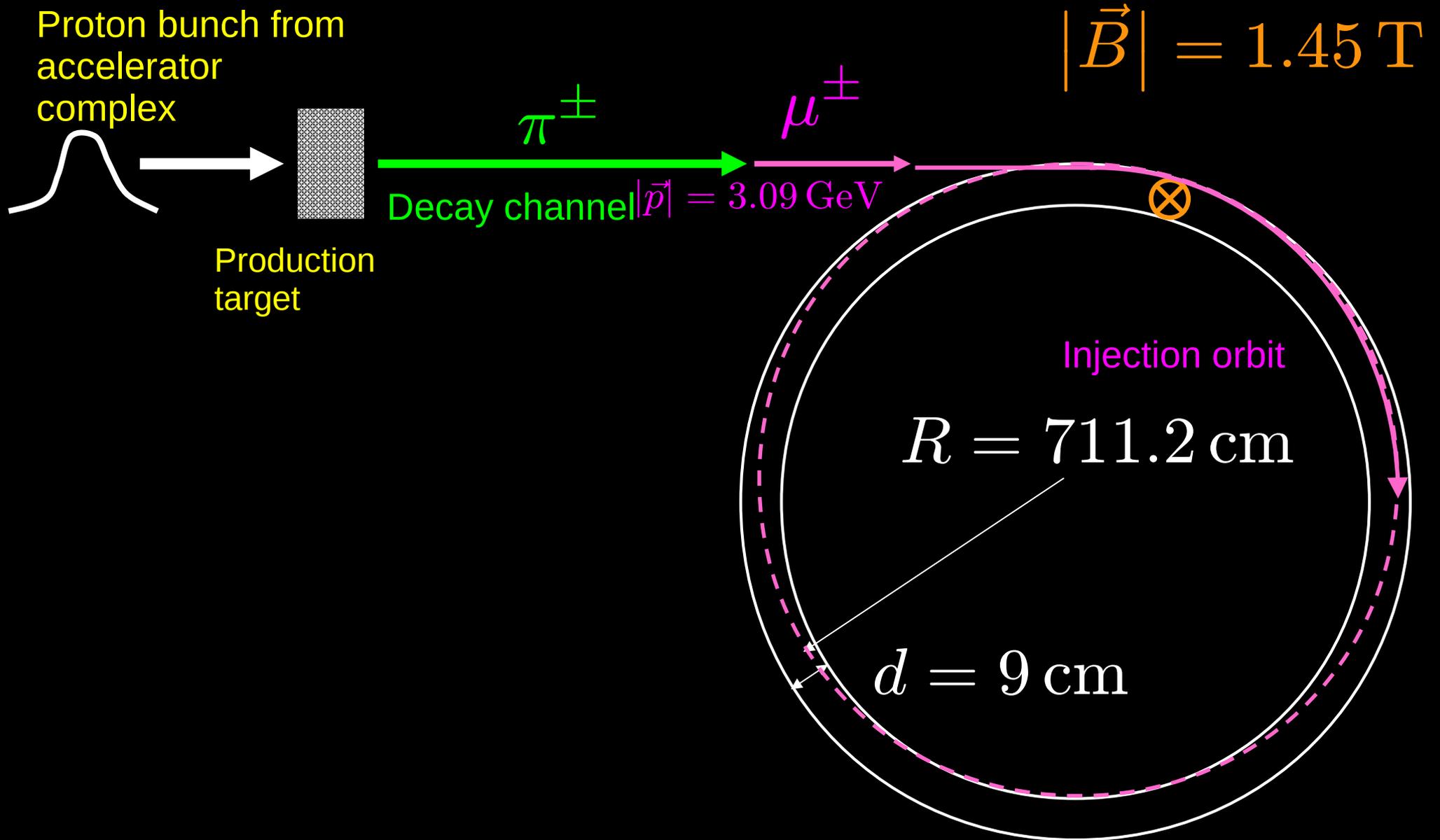
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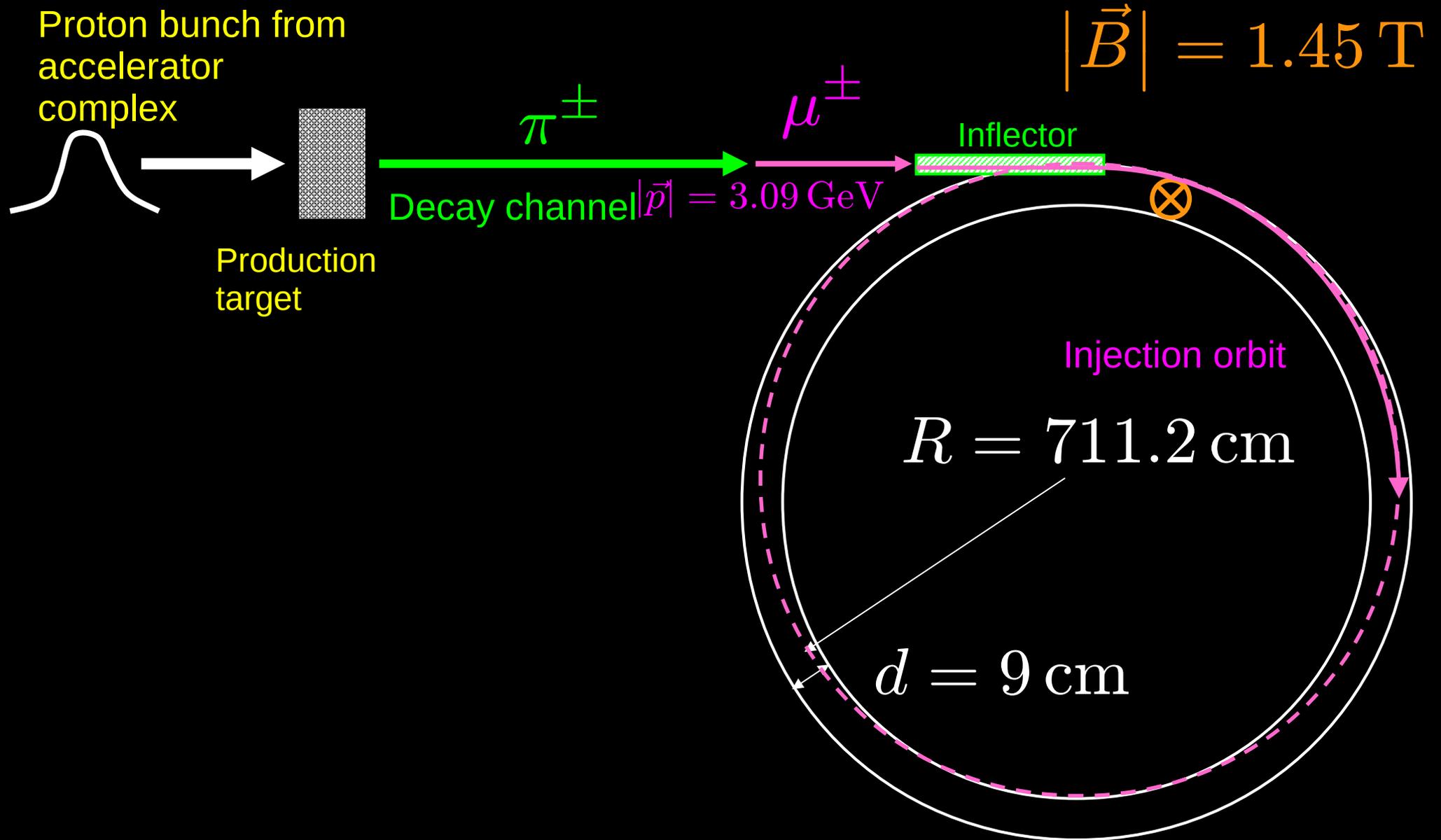
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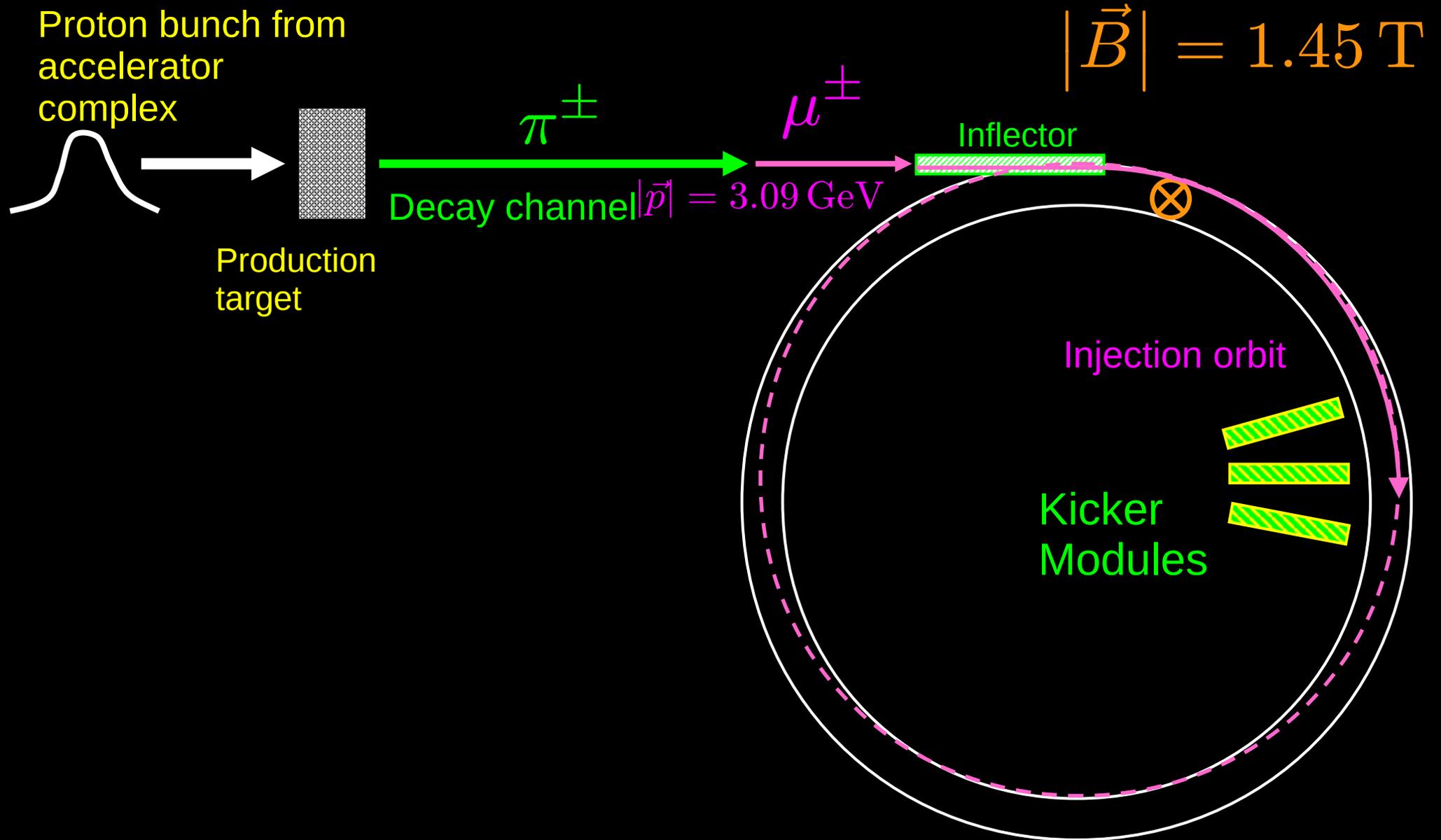
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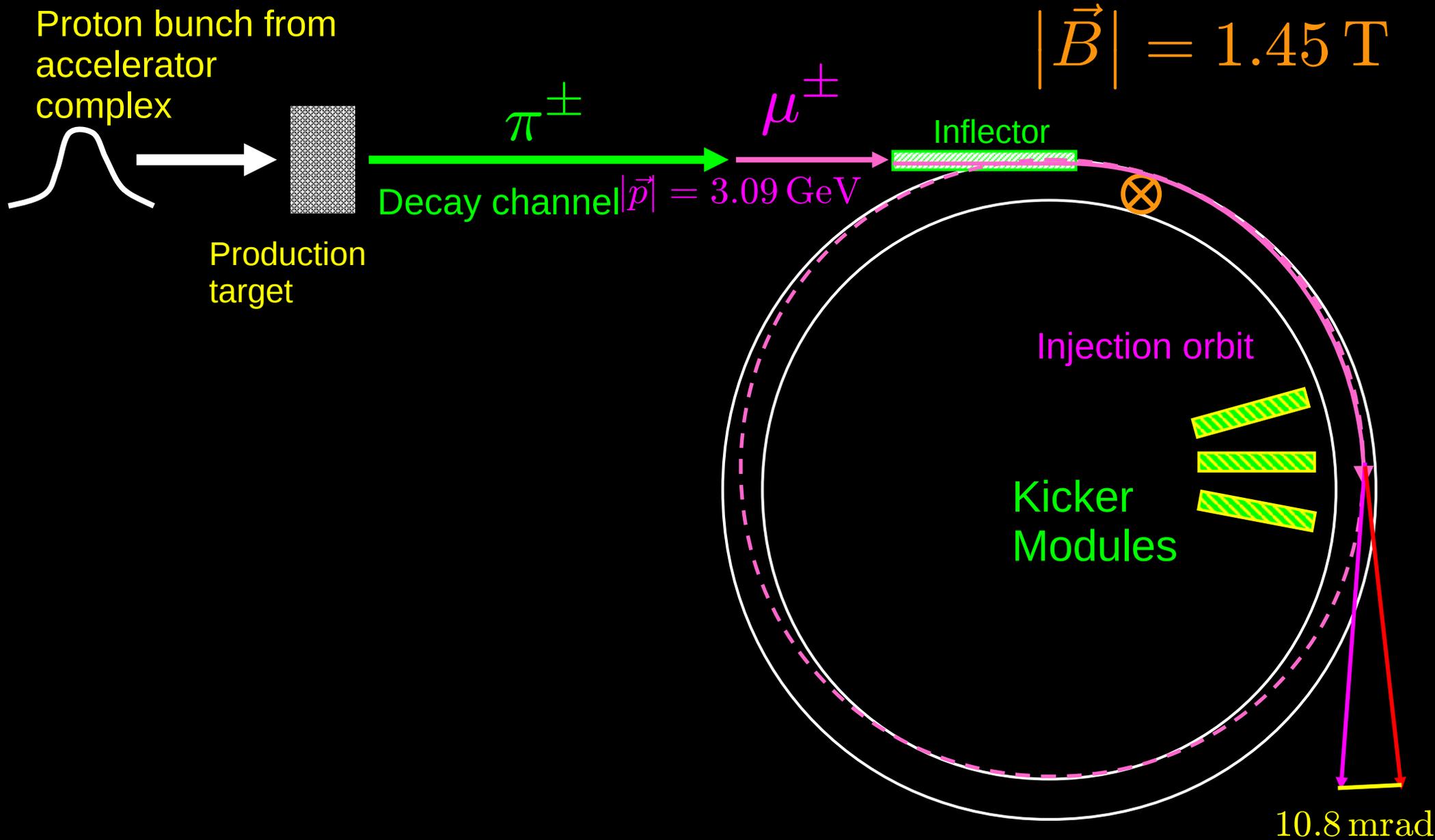
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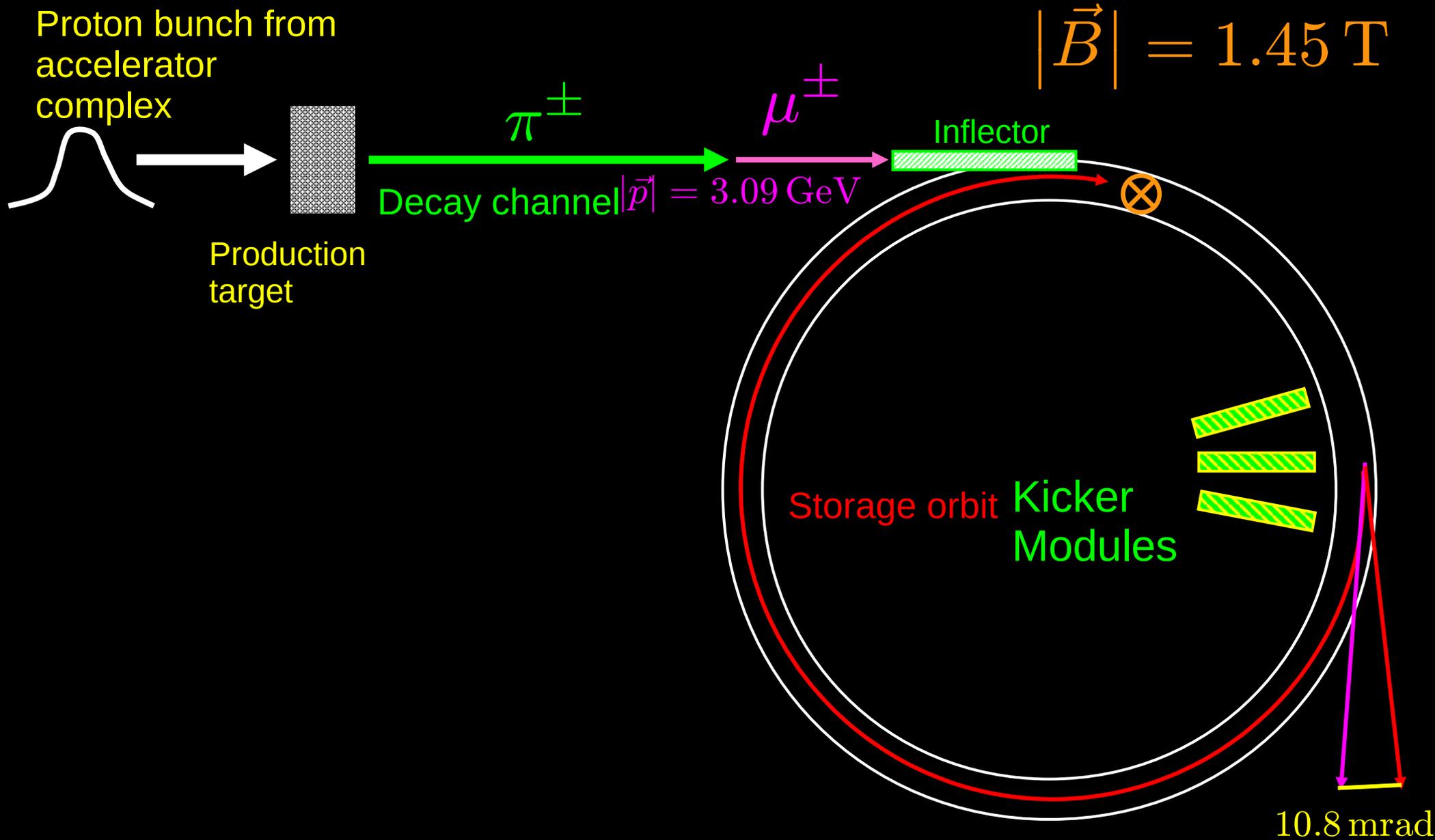
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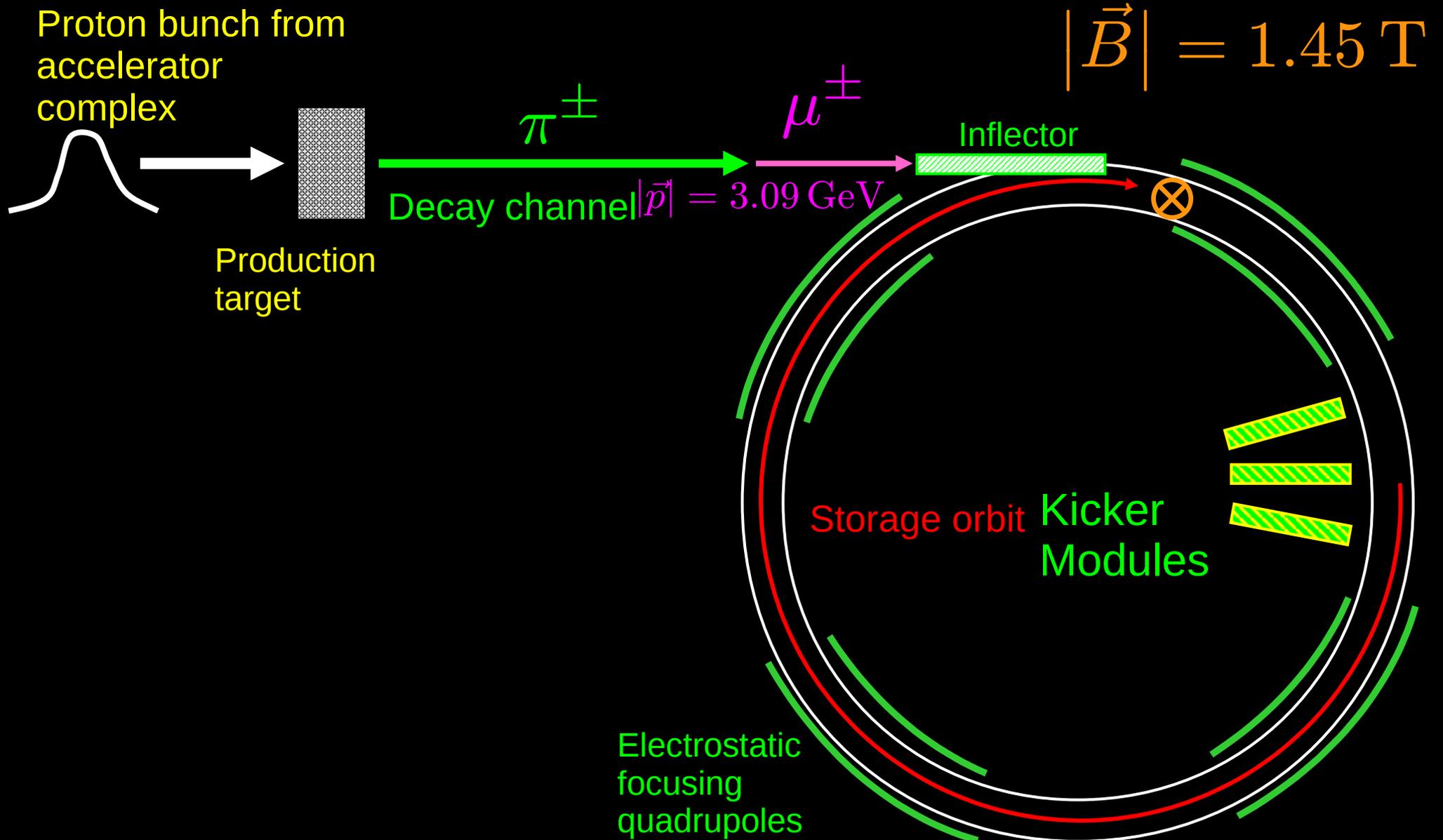
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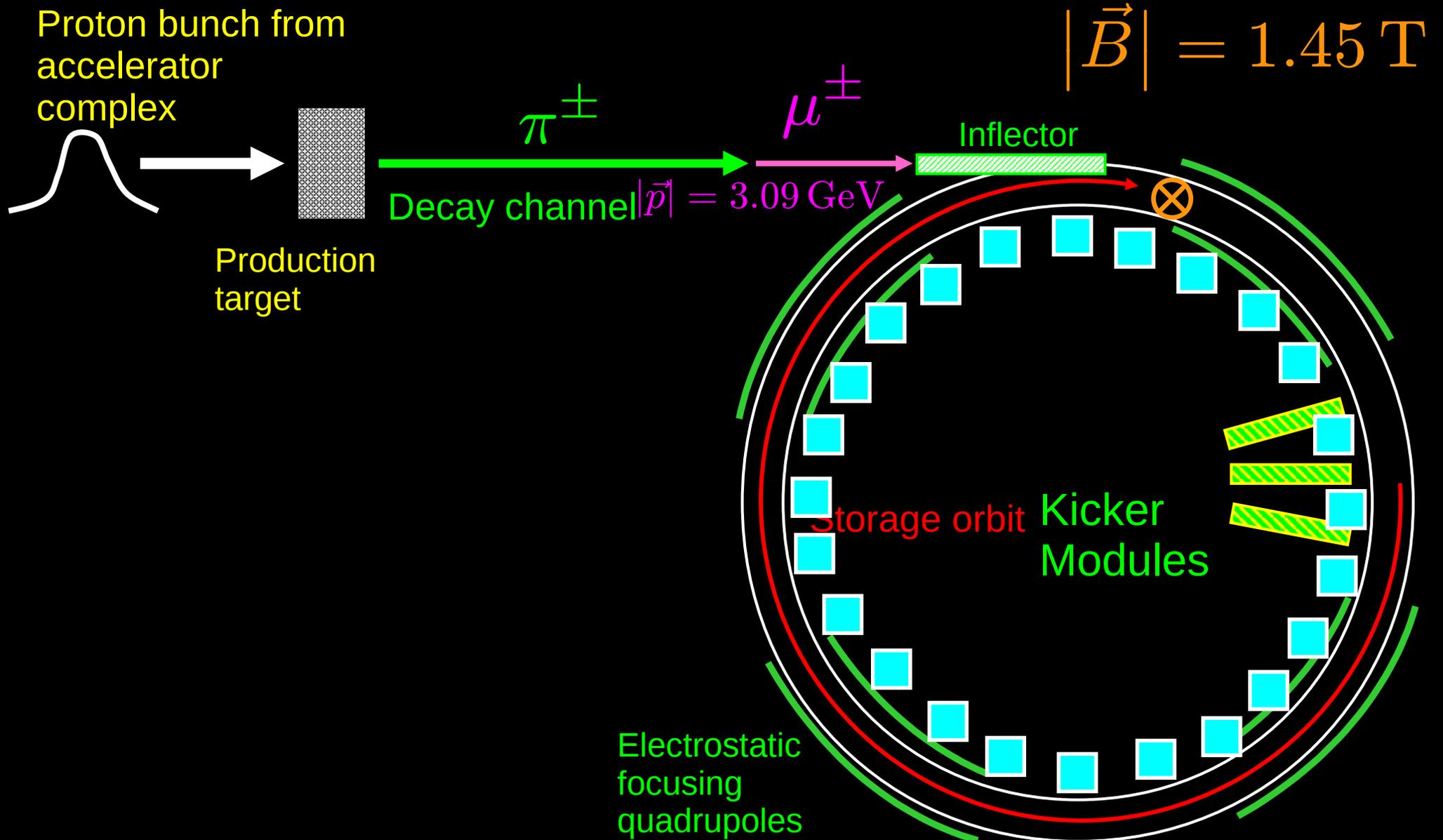
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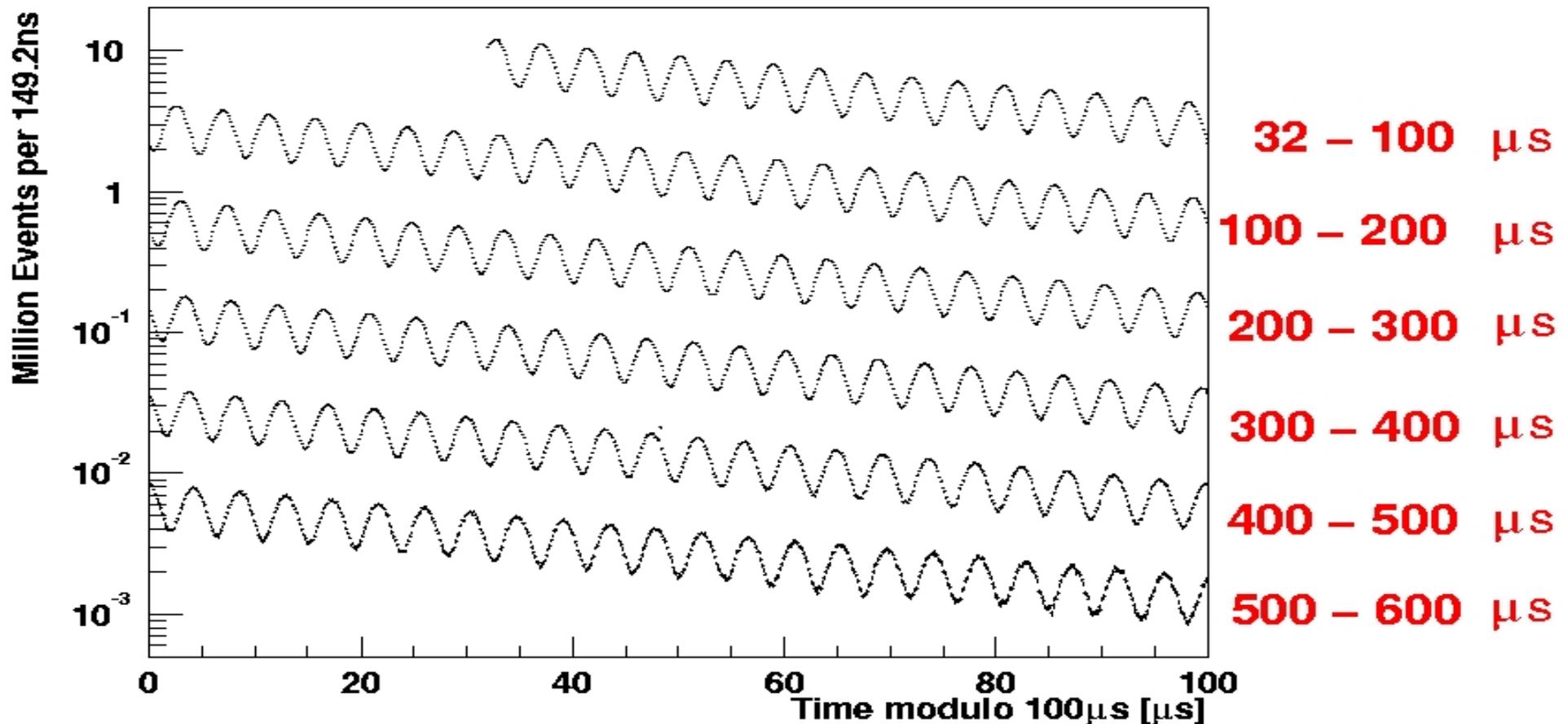
# Experimental Technique



We measure the electron energies,  
choose a cutoff, and fit for  $\omega_a$  ...

$$f(t) = N_0(E)e^{-t/\tau} [1 + A(E) \cos(\omega_a t + \phi)]$$

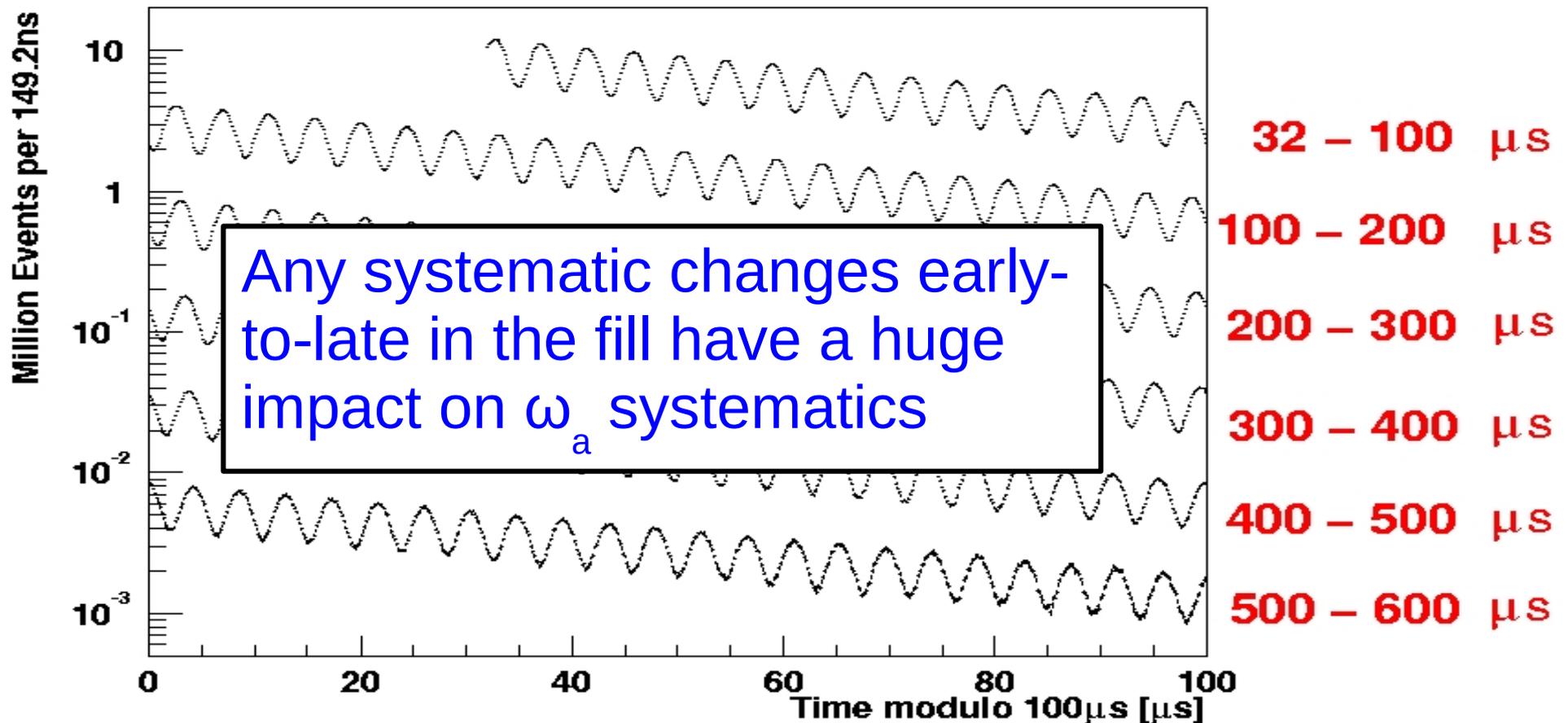
**electron time spectrum (2001)**



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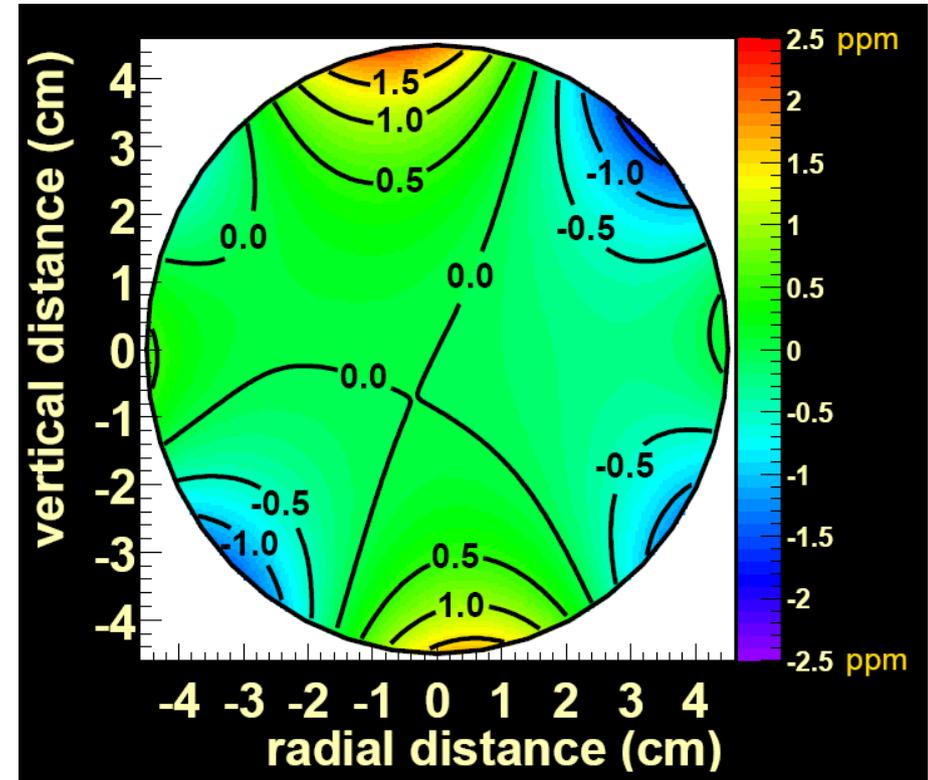
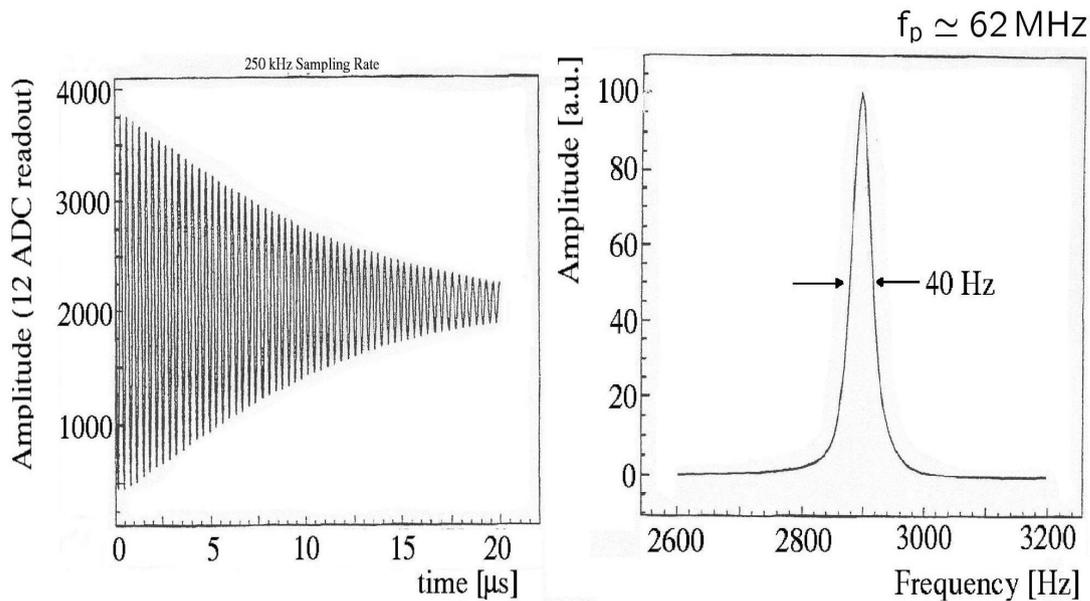
### electron time spectrum (2001)



# We simultaneously find the magnetic field with a frequency measurement

Pulsed NMR and FID of protons with mobile and fixed probes measure the Larmor frequency,  $\omega_p$ , in the storage field.

Free induction decay signals:



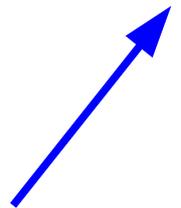
The B-field at E821 was uniform at the 1ppm level with uncertainty on  $\langle B \rangle$  is less than 0.03ppm

Finally, combine the omegas to get a result

$$\omega_a = \left( \frac{eB}{m_\mu} \right) \frac{g_\mu - 2}{2} \qquad \omega_p = \left( \frac{eB}{2m_p} \right) g_p$$

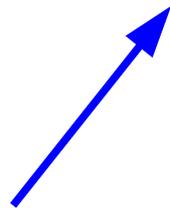
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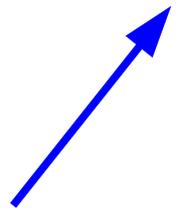
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$$a_\mu = 11\,659\,208(6) \times 10^{-10} \quad (0.54 \text{ ppm})$$

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$$\sigma_{\text{BNL}} = \left\{ \begin{array}{l} 0.46 \text{ ppm statistical} \\ 0.28 \text{ ppm systematic} \end{array} \right\} = 0.54 \text{ ppm}$$

To do better using this technique, requires many small improvements in a lot of areas

## Field Systematics:

Source of uncertainty	R99 [ppb]	R00 [ppb]	R01 [ppb]	E989 [ppb]
Absolute calibration of standard probe	50	50	50	35
Calibration of trolley probes	200	150	90	30
Trolley measurements of $B_0$	100	100	50	30
Interpolation with fixed probes	150	100	70	30
Uncertainty from muon distribution	120	30	30	10
Inflector fringe field uncertainty	200	–	–	–
Time dependent external $B$ fields	–	–	–	5
Others †	150	100	100	30
Total systematic error on $\omega_p$	400	240	170	70
Muon-averaged field [Hz]: $\tilde{\omega}_p/2\pi$	61 791 256	61 791 595	61 791 400	–

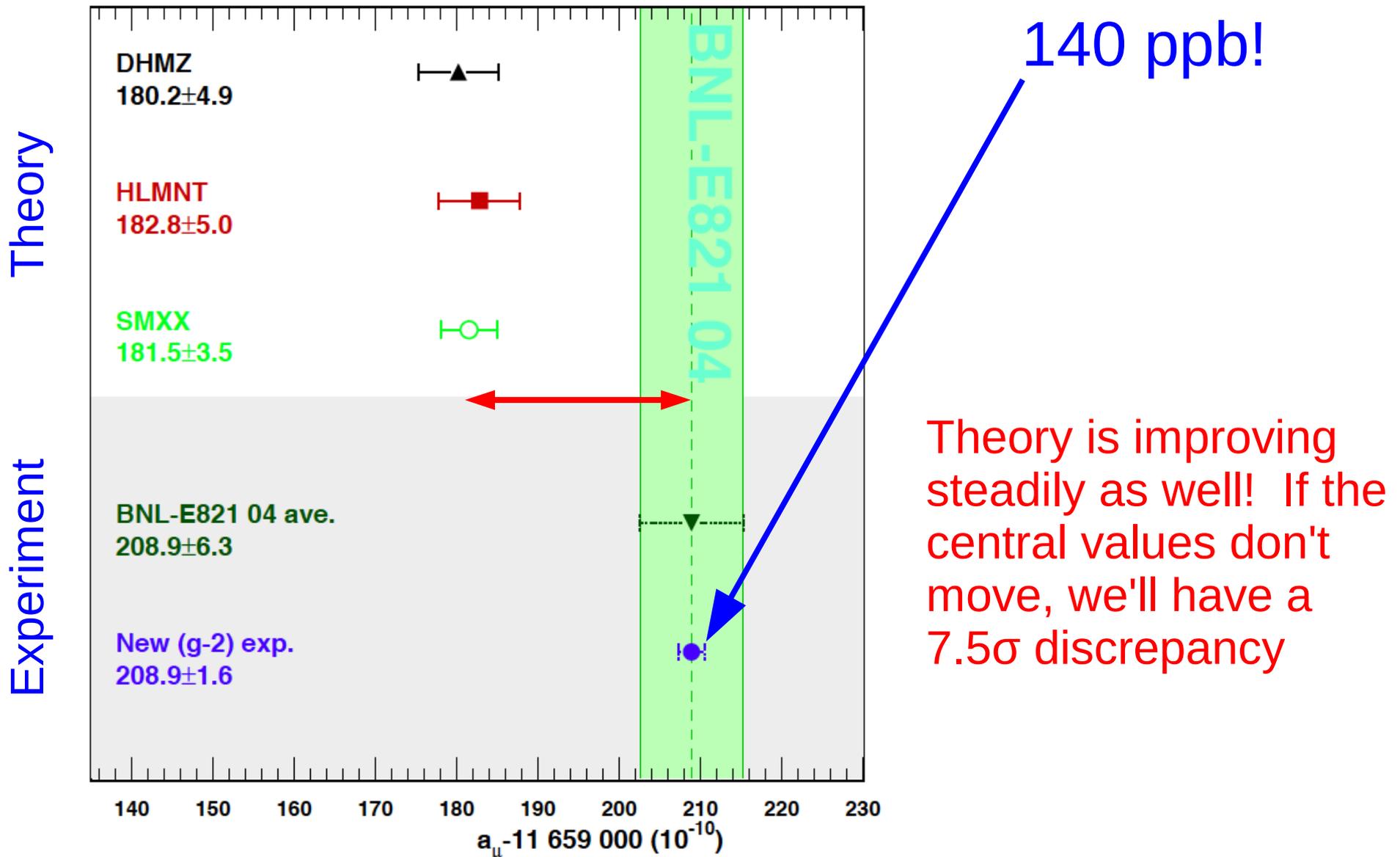
- † Higher multipoles, trolley temperature ( $\leq 50$  ppb/ $^{\circ}$  C) and power supply voltage response (400 ppb/V,  $\Delta V=50$  mV), and eddy currents from the kicker.

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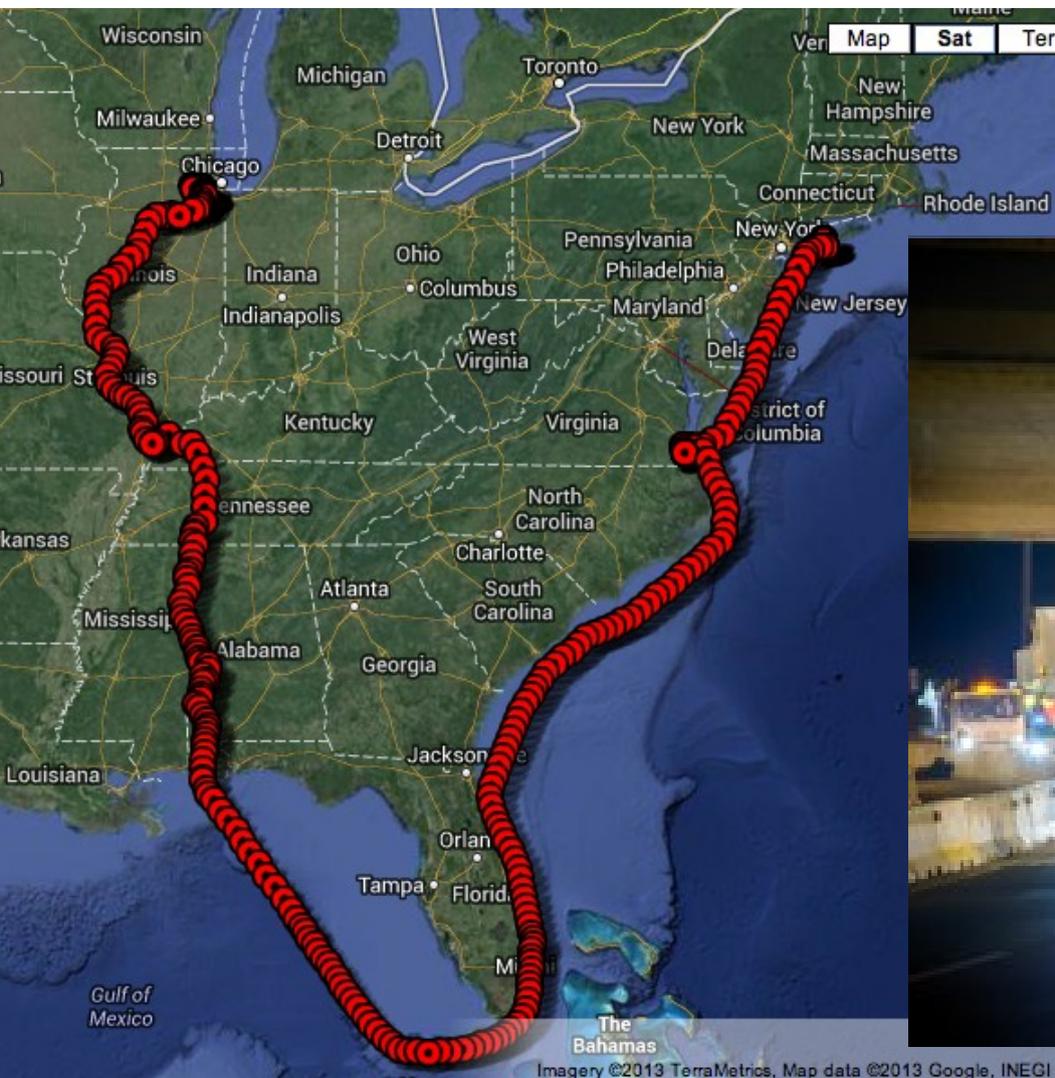
## Precession Systematics:

Category	E821 [ppb]	E989 Improvement Plans	Goal [ppb]
Gain changes	120	Better laser calibration	
		low-energy threshold	20
Pileup	80	Low-energy samples recorded	
		calorimeter segmentation	40
Lost muons	90	Better collimation in ring	20
CBO	70	Higher $n$ value (frequency)	
		Better match of beamline to ring	< 30
$E$ and pitch	50	Improved tracker	
		Precise storage ring simulations	30
Total	180	Quadrature sum	70

Along with the additional statistics, the total uncertainty will improve by a factor of 5



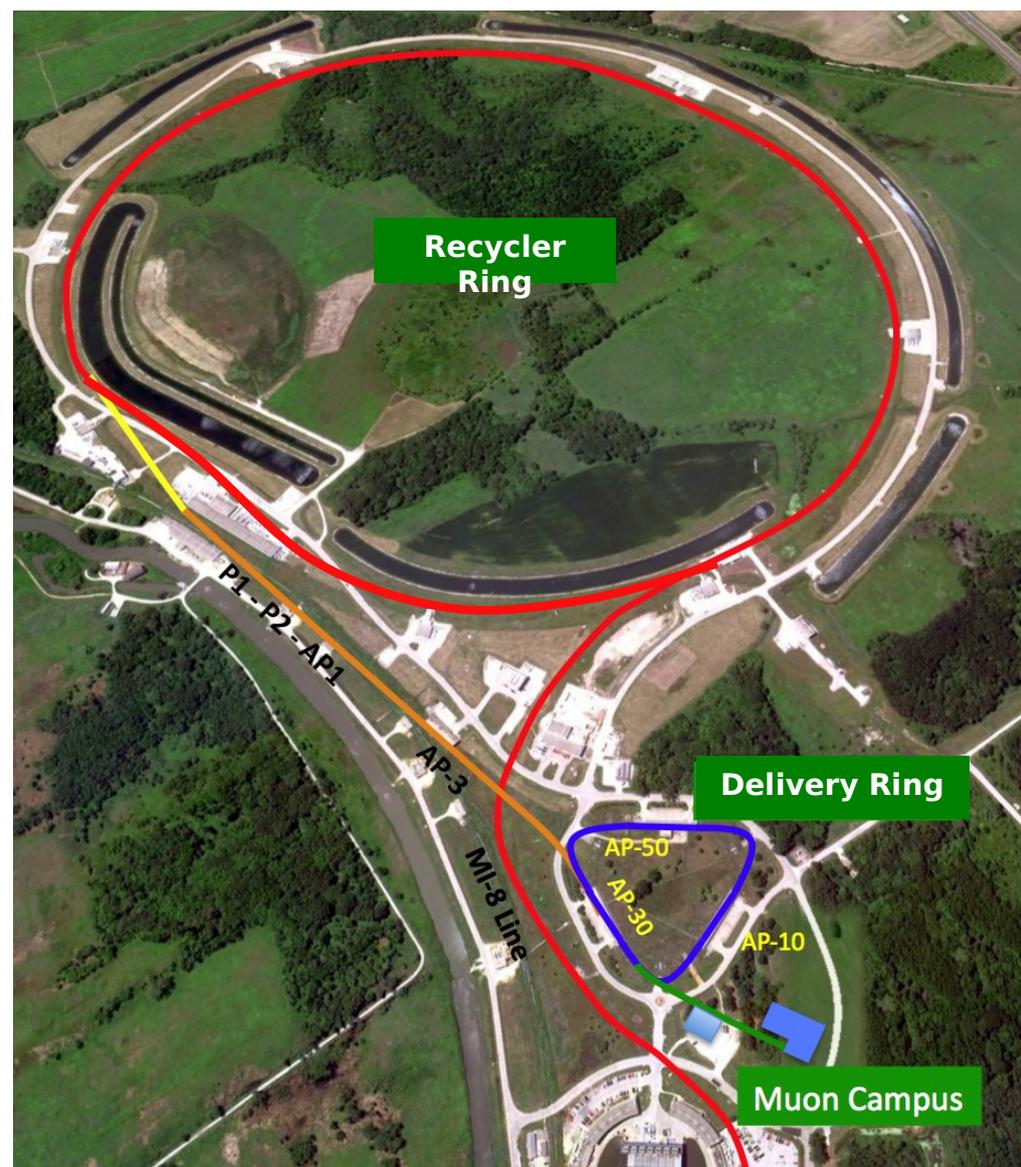
# The first step was moving the ring from BNL to FNAL ...



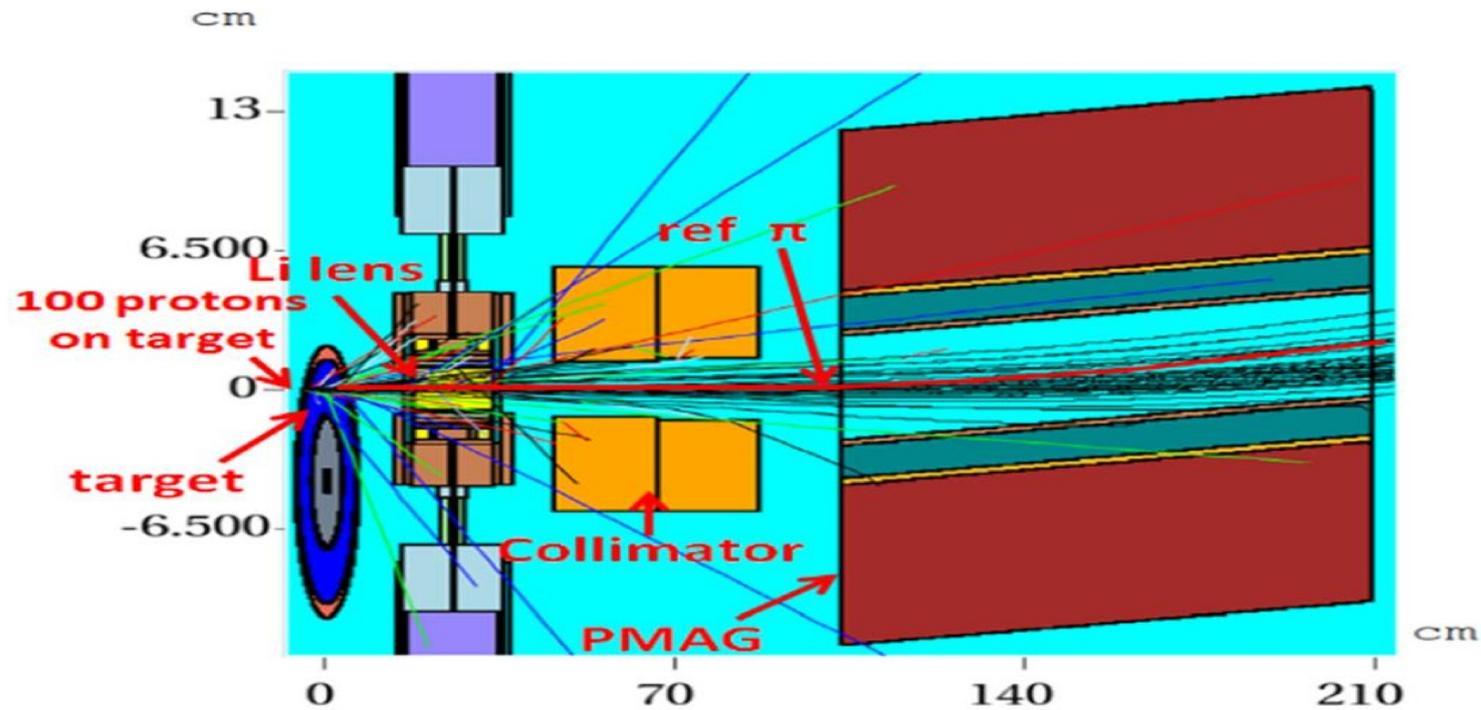
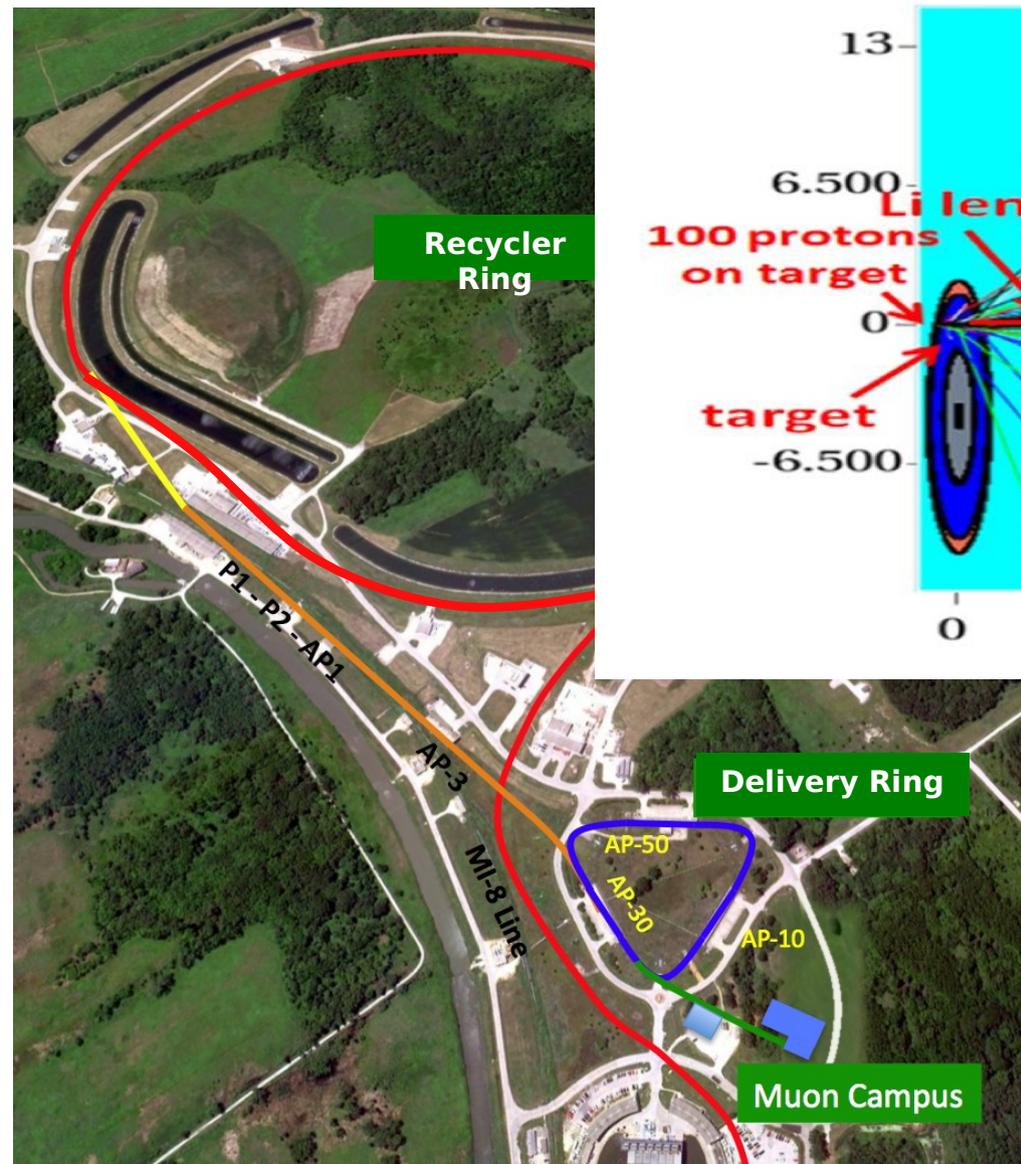
... and giving it a new home



# We need a new, highly polarized muon source

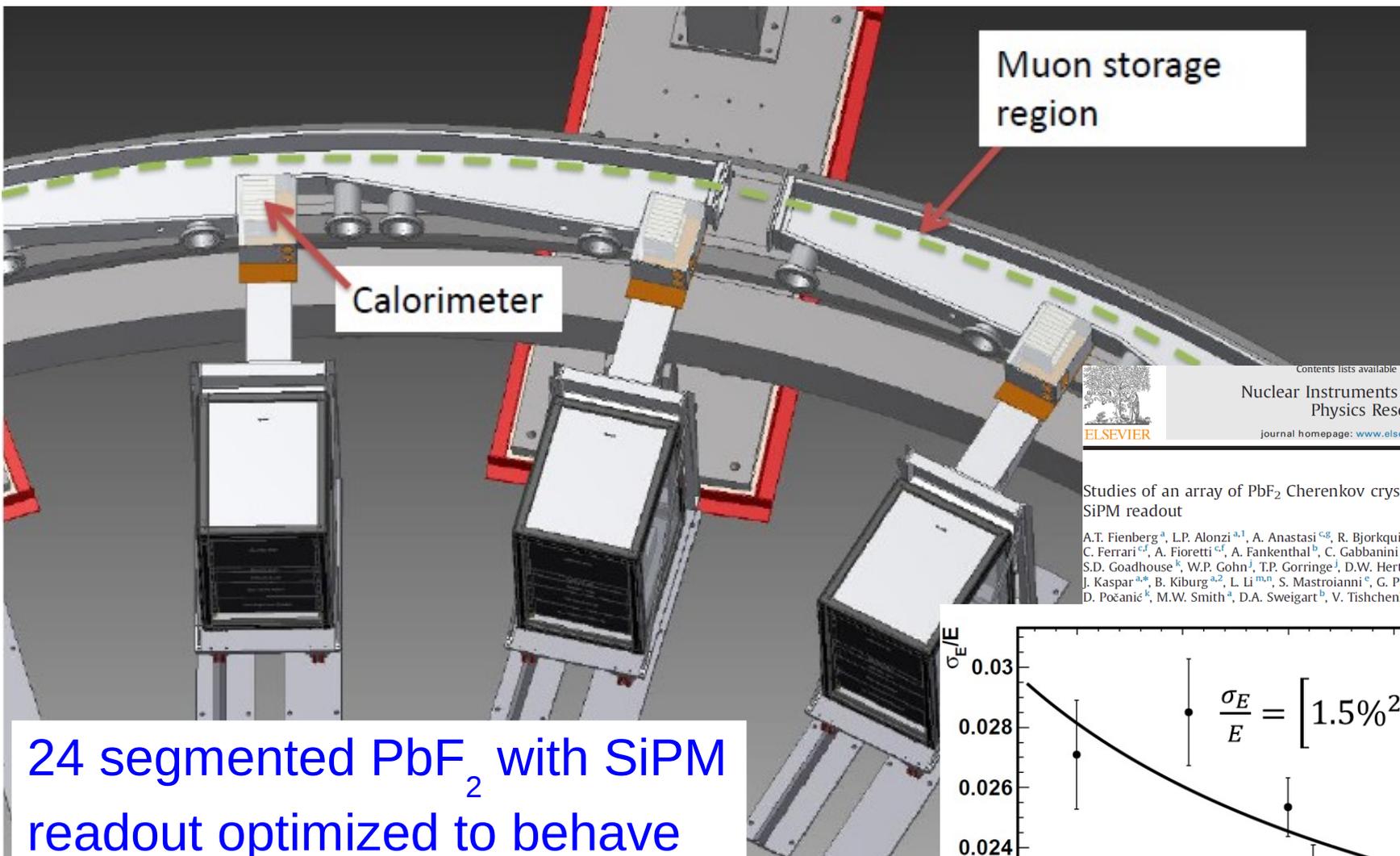


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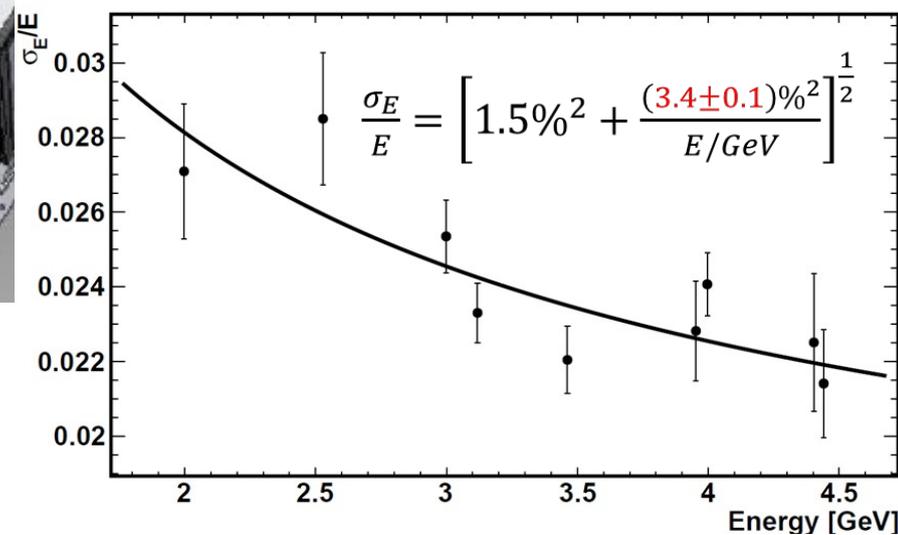


The original antiproton source becomes the g-2 pion production target station, while the delivery ring acts as a pion decay channel

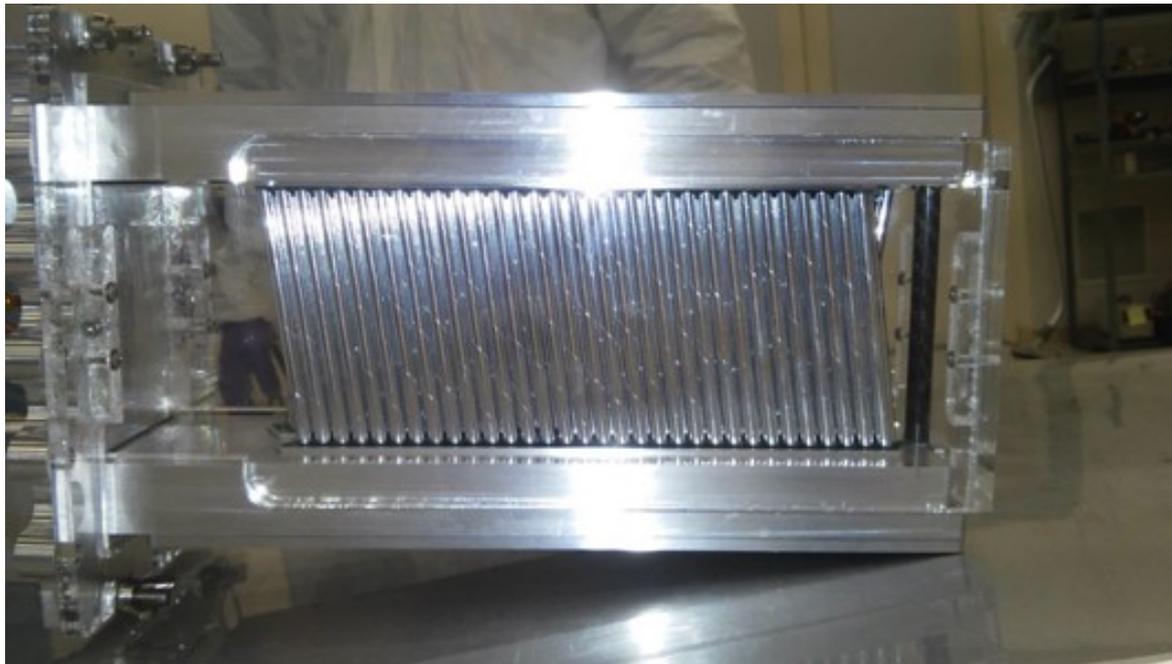
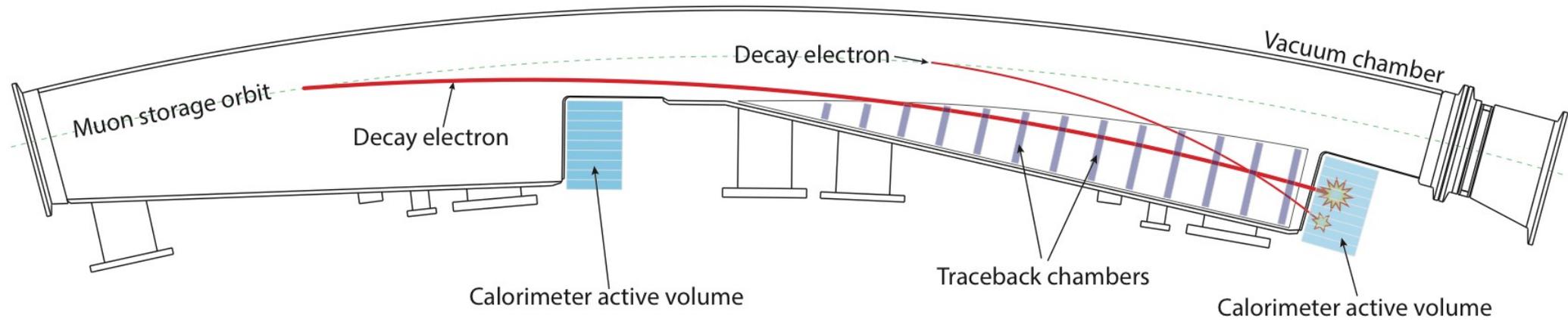
# The detector systems will be all new



24 segmented PbF<sub>2</sub> with SiPM readout optimized to behave like short pulse duration PMTs to minimize pileup and excellent resolution



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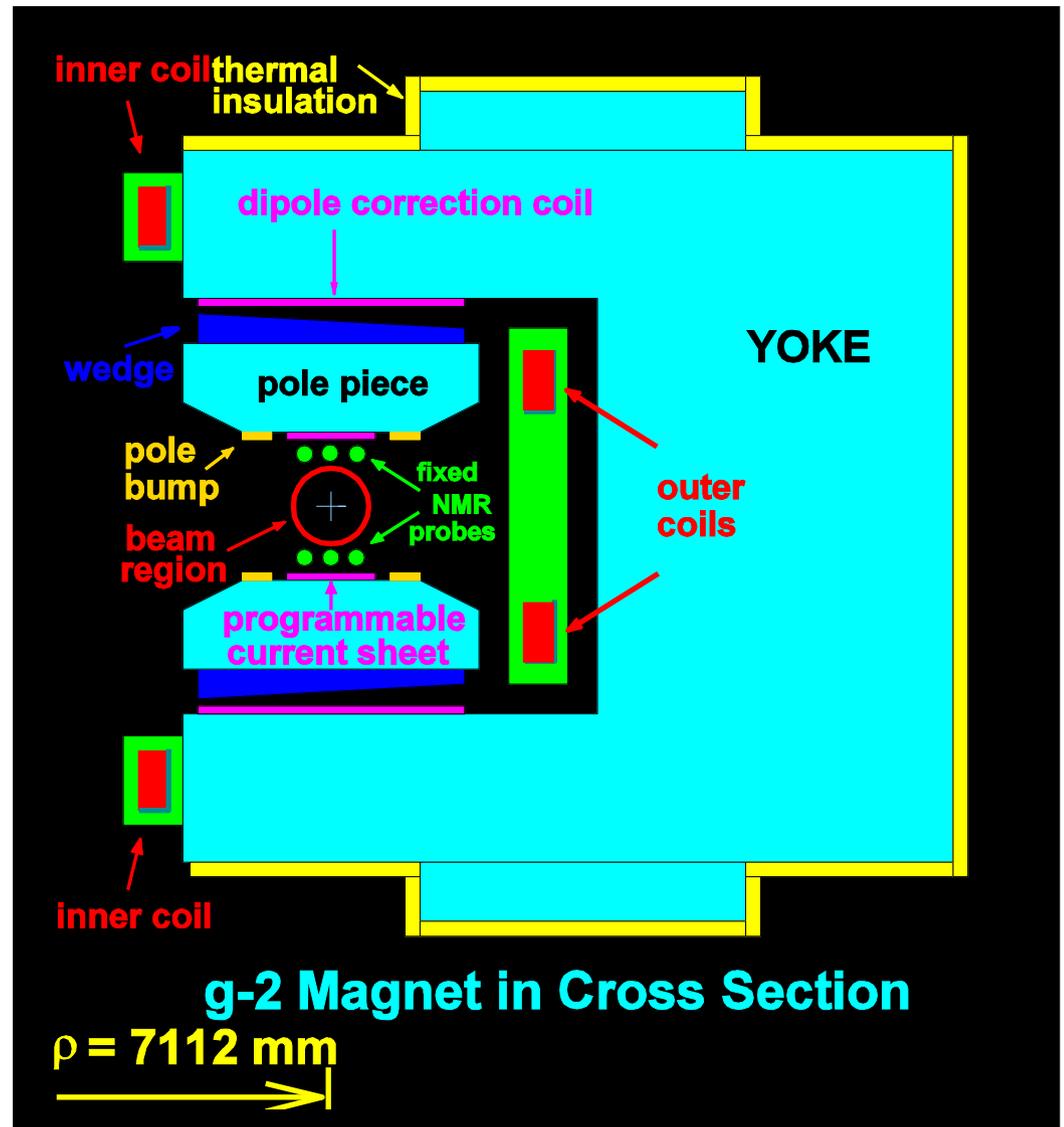
Three multiplane straw tracker systems will reconstruct the time-dependent muon decay position within the ring

# There are numerous improvements to both the field and field measurements



New fixed and mobile field mapping probes

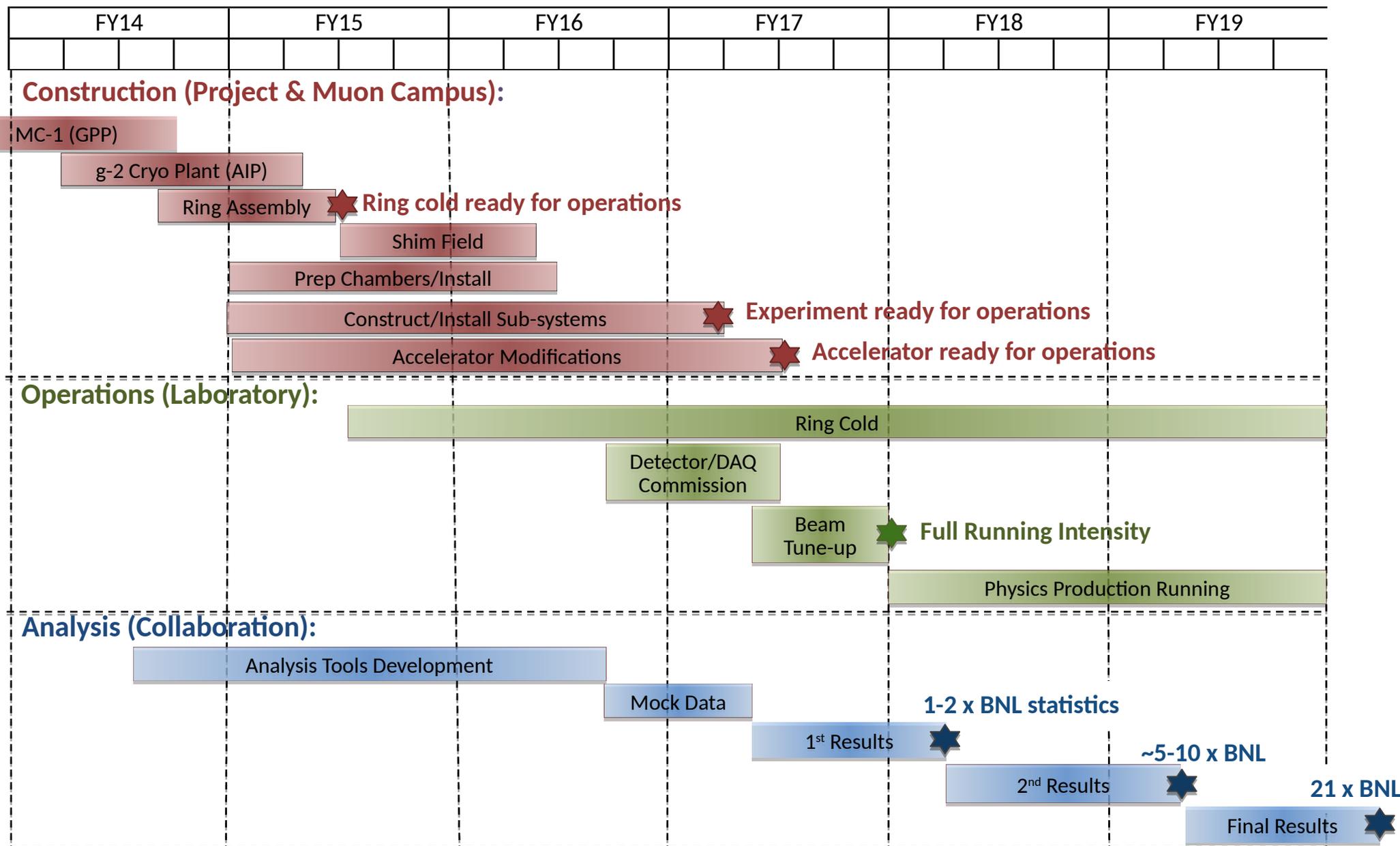
Improved temperature control, passive shimming, and active low order multipole correction



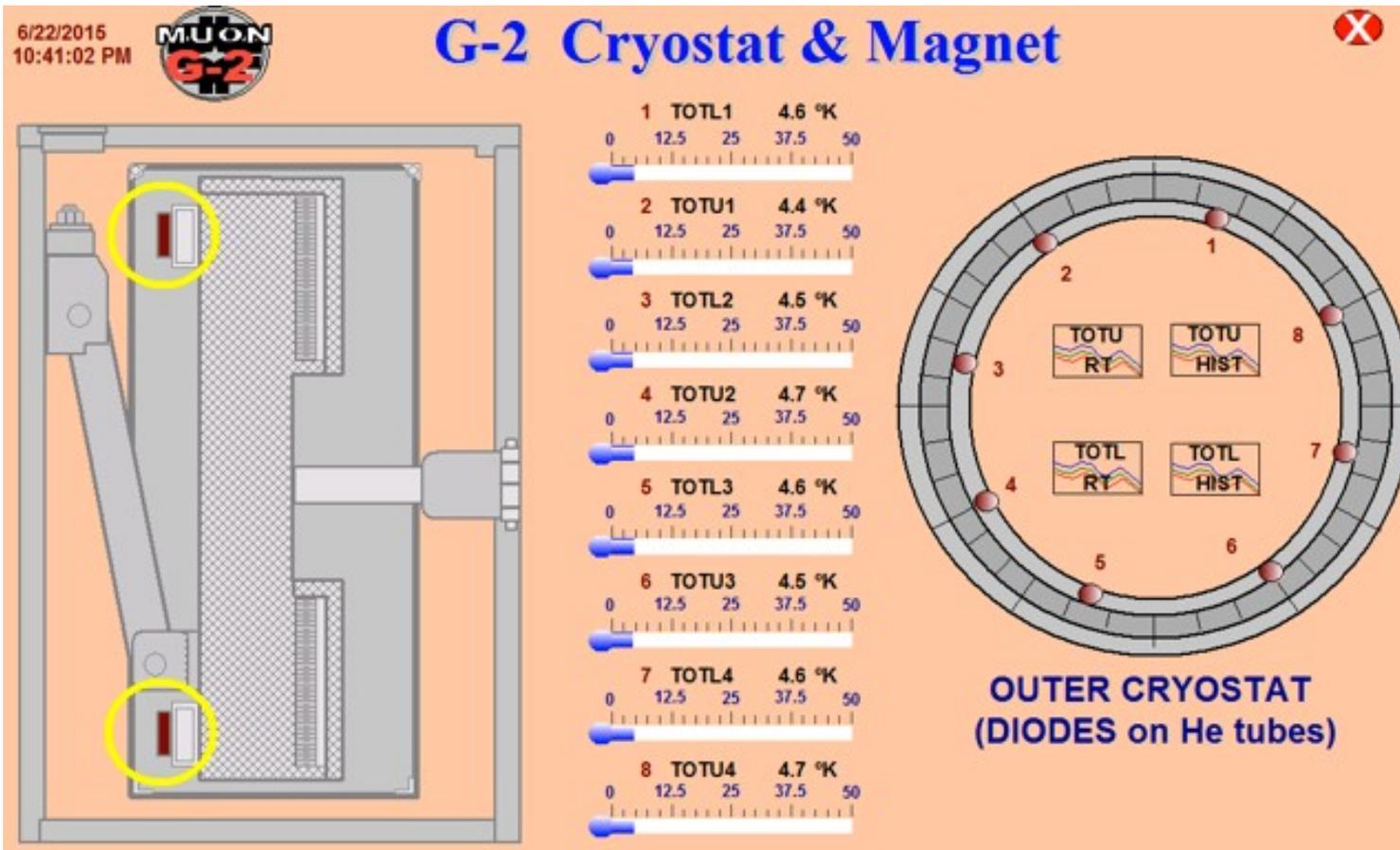
Compared to E821, there are a whole host of other improvements too numerous to discuss

- New quadrupoles
- New kicker modules
- New absolute field calibration
- New trolley field calibration system
- New detectors to measure beam profiles
- New analysis algorithms
- More complete simulation framework
- New data acquisition hardware
- New data acquisition software
- New laser gain stabilization system

# Schedule



# Recent significant progress

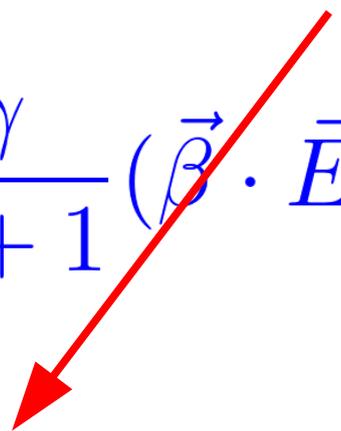


After 14 years, the ring has been cooled to superconducting temperatures and partially energized; some inevitable teething problems have been fixed, and the cooling should begin again on Monday

We can do other muon physics in parallel: EDMs, Lorentz Violation searches

$$\vec{\omega}_e = -\frac{\eta e}{2mc} \left( \vec{E} + \vec{\beta} \times \vec{B} - \frac{\gamma}{\gamma + 1} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right)$$

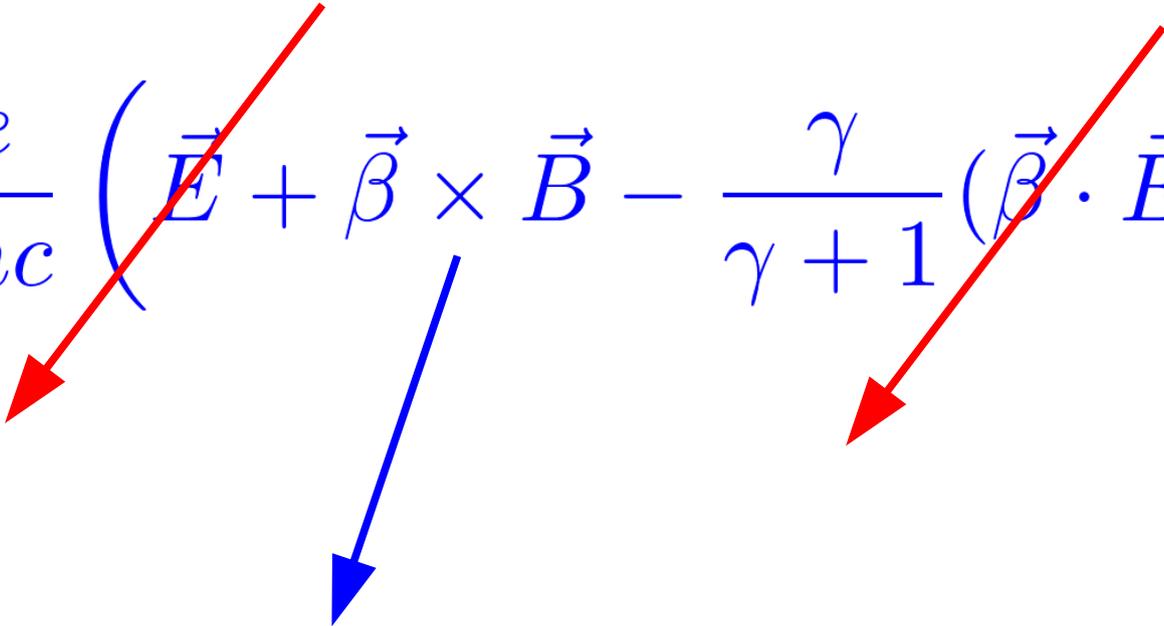
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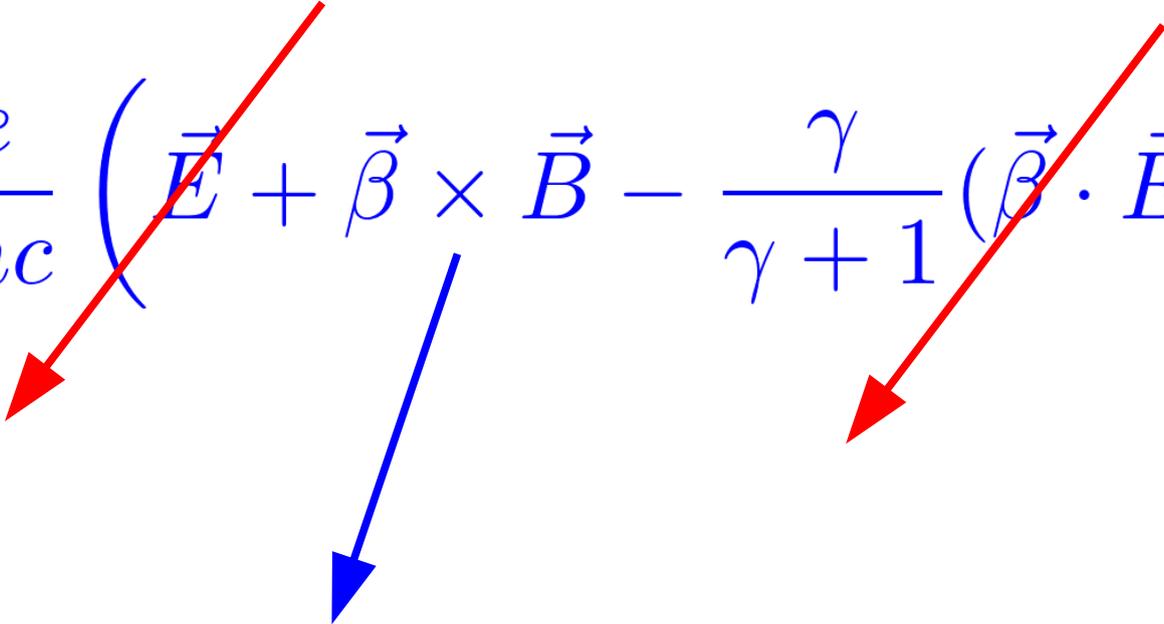
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A diagram with three arrows pointing from the equation to the text below. Two red arrows point from the terms  $\vec{E}$  and  $(\vec{\beta} \cdot \vec{E}) \vec{\beta}$  to the text. A blue arrow points from the term  $\vec{\beta} \times \vec{B}$  to the text.

Causes an out of plane rotation that is in phase with the g-2 precession!

The trackers are designed to enable a measurement of this rotation; we expect a 100 fold improvement over the E821 value using the same method due to greater statistics.

Thanks for your continuing interest!

